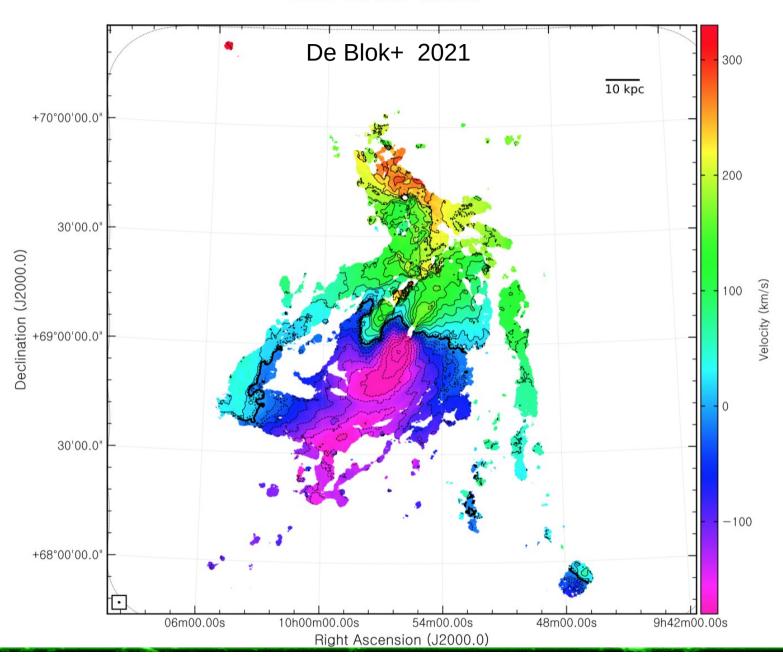
# The Interstellar Medium (ISM)

HI IN THE M81 TRIPLET



# The Interstellar Medium (ISM): outline

The radio view, what radio astronomy can measure

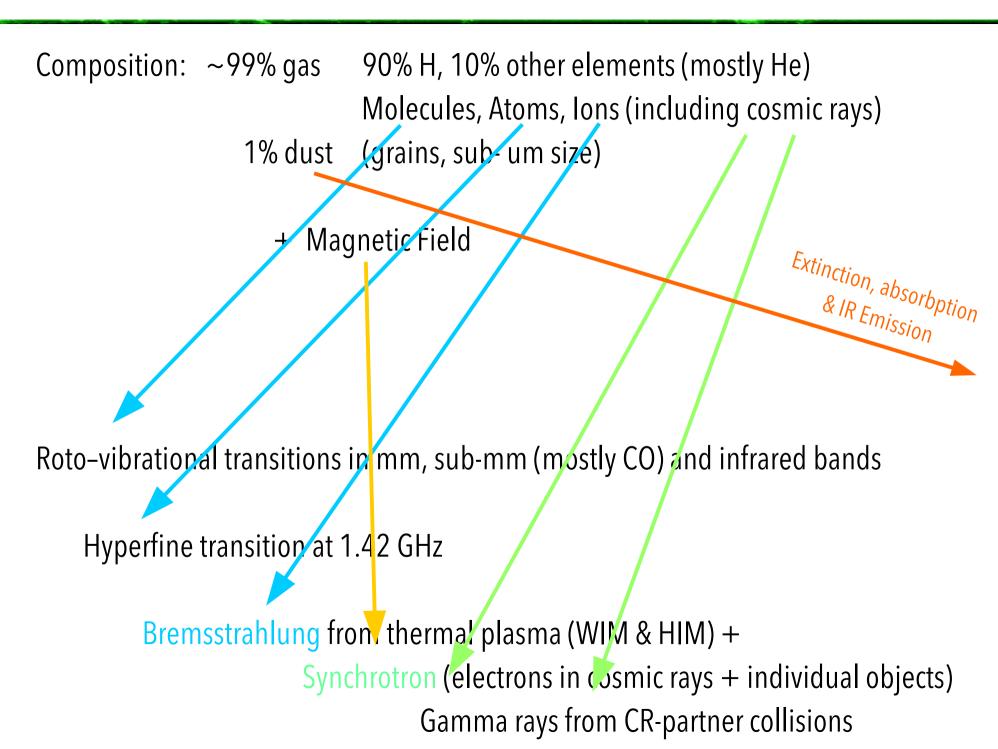
Main research fields

A number of open questions

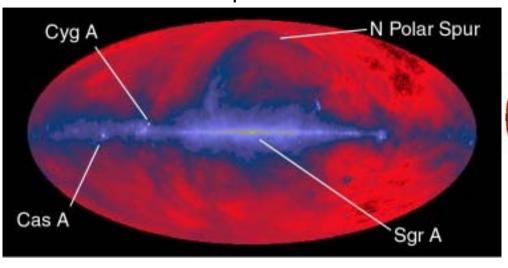
- Fanti & Fanti § 13
- Tools of Radio Astronomy § 13

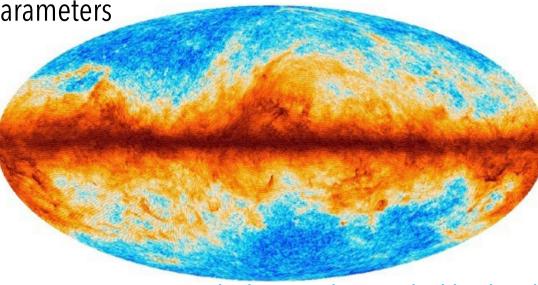
- What is it? Composition, Observations, Parameters
- > HII
- > HI
- Masers & Stars (circum stellar envelopes)
- > H<sub>2</sub> (CO & al.)

Spirals .vs. Ellipticals (& Irregulars)

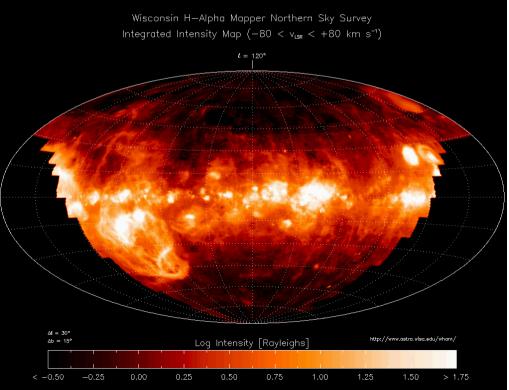


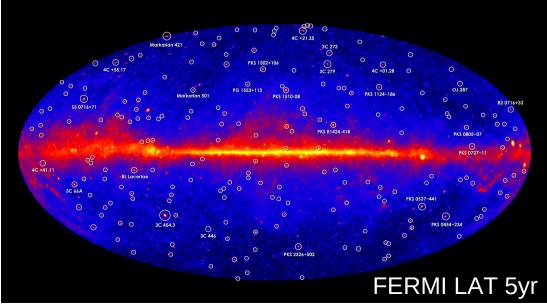
What is it? Composition, Observations, Parameters





Dust emission as observed with Planck





#### The Interstellar Medium (ISM)

What is it? Composition, Observations, Parameters

Average density 0.1-1 cm<sup>-3</sup>, inhomogeneous distribution

Name	N (cm <sup>-3</sup> )	T (K)	M (10 <sup>9</sup> M <sub>sun</sub> )	Fraction of Total Volume
molecular	> 10 <sup>2</sup>	10	2	1%
CNM	50	< 10 <sup>2</sup>	3	4%
WNM	0.5	10 <sup>3</sup>	4	30%
WIM	0.3	10 <sup>4</sup>	1	15%
HIM	0.003	>10 <sup>6</sup>	0.1	50%

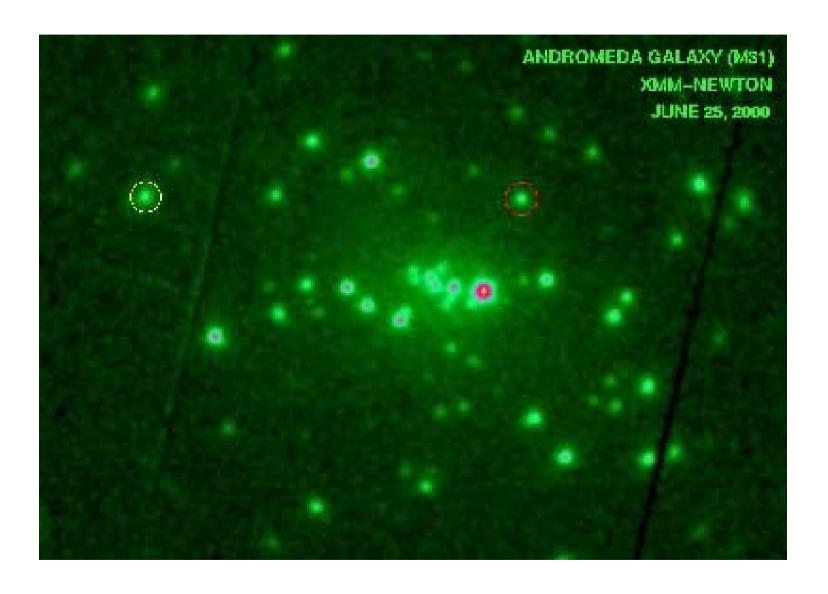
Typical values for a spiral galaxy

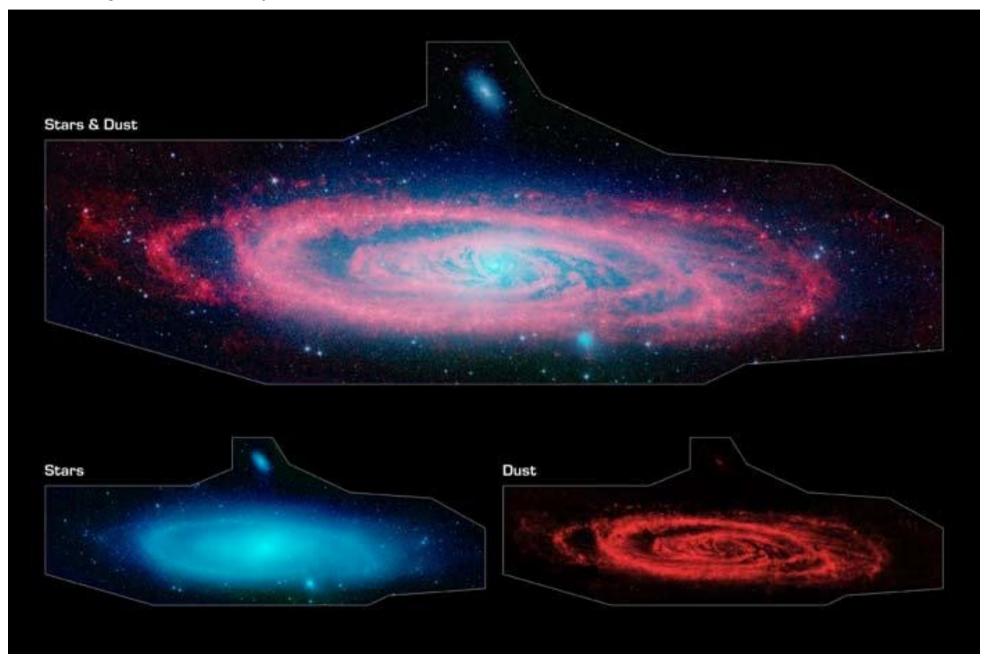
Dust is generally associated with CNM, i.e. dense and cold environments

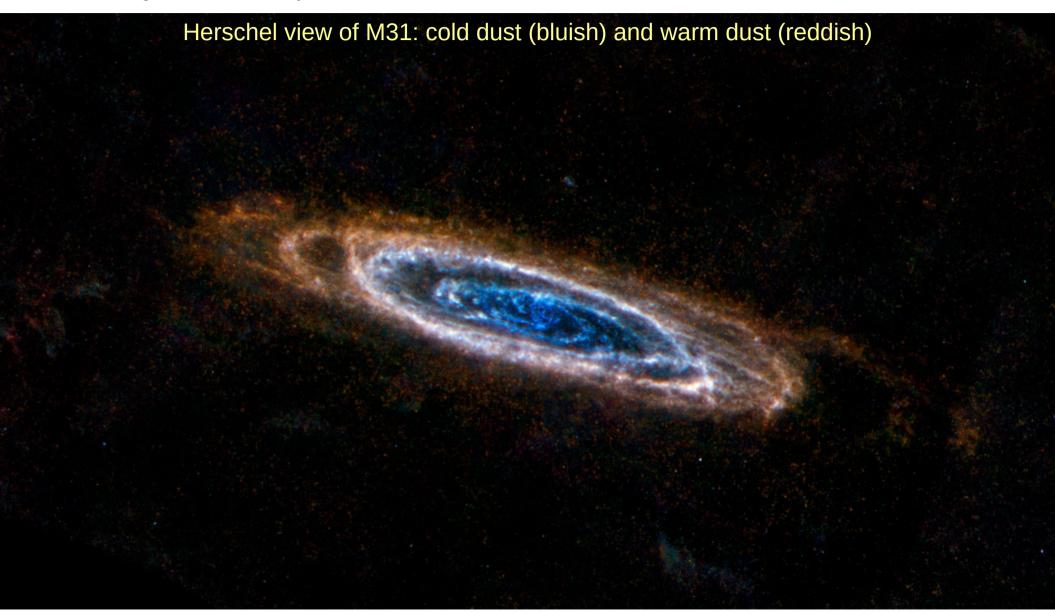
Learning from other spirals: M 31 aka Andromeda Galaxy, ~3.2° x 1.0° in size



Learning from other spirals: X – rays captured by XMM – Newton (30' FoV)

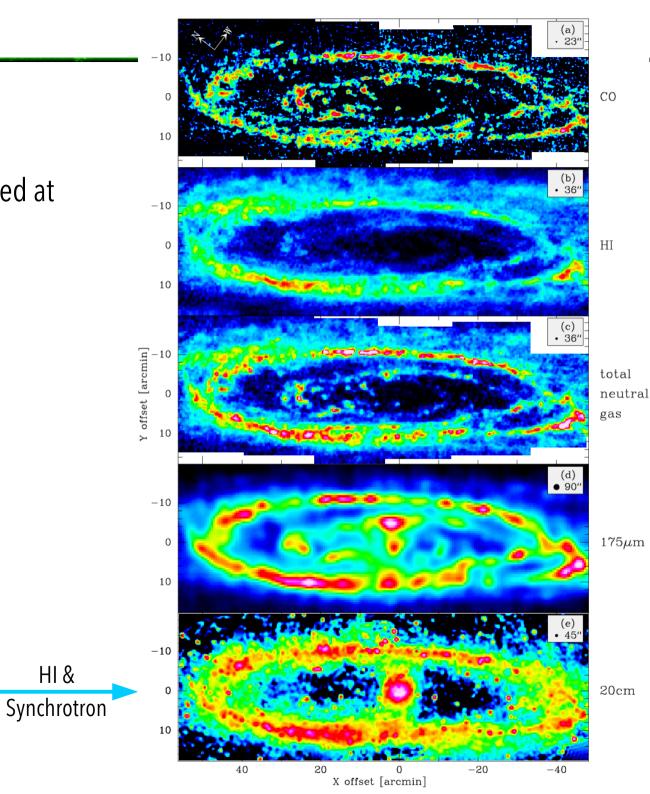


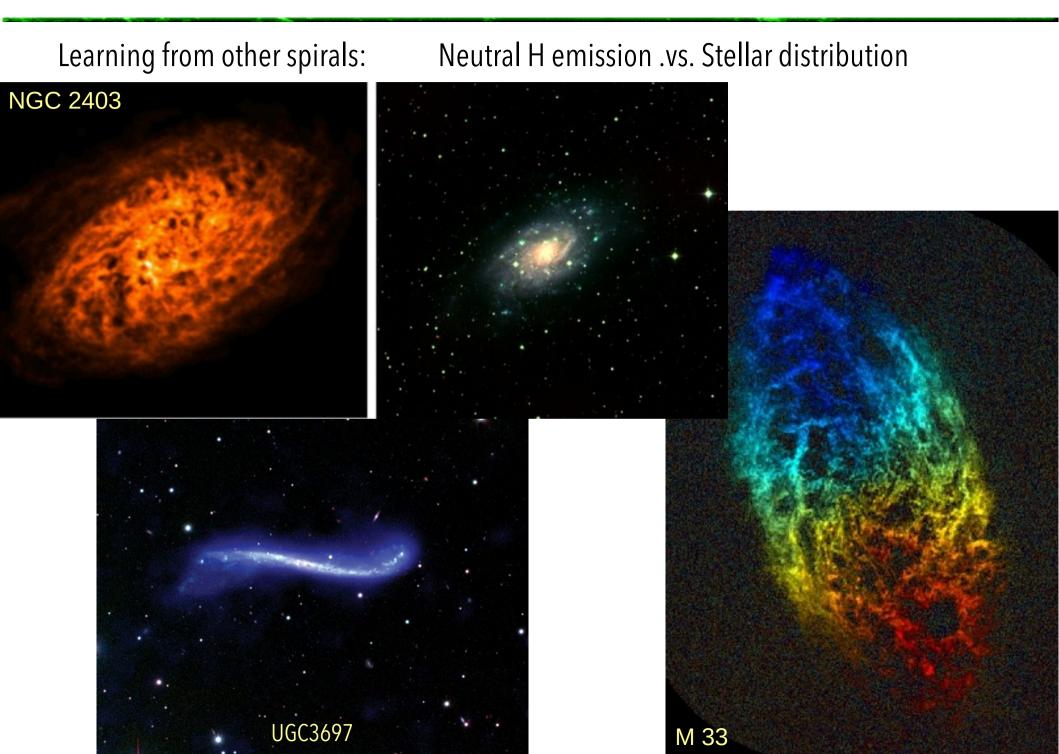




Comparison of emission observed at different wavelenghts

HI &





Purple: VLA

Red: Spitzer

Yellow: DSS

Blue: Chandra



#### Neutral Hydrogen

- > Hyperfine structure:  $\Delta E \sim 5.9 \mu eV$
- > Natural width of 21 cm line  $\sim 10^{-16}$  m/s
- Collisions ~ 10<sup>4</sup> times more frequent than radiative transitions, then thermal equilibrium
- Excited level : Ground level = 3 : 1

# The brightness temperature derived from line photons:

$$T_{B(H)} = T_s(1-e^{-\tau_H})$$
 where  $\tau_H$  is the optical depth

If 
$$\tau_H \ll 1 \rightarrow T_{B(H)} = T_s \tau_H$$

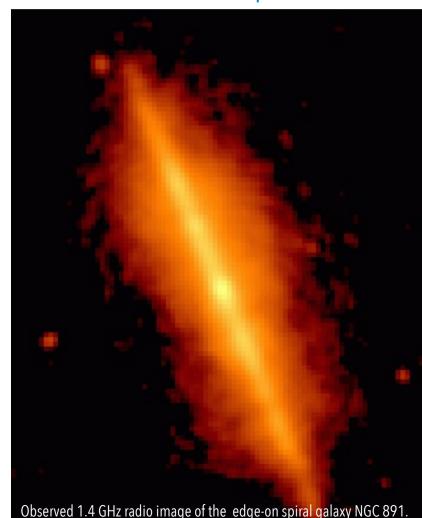
$$T_{B(H)}$$
 is in K if  $N_{H}$  is in cm<sup>-2</sup>

$$n_{\mu}I = N_{\mu}$$
 column density

$$T_{B(H)} = \int_{\text{line}} T_{B(H)}(\mathbf{v}) d\mathbf{v} = \int_{\text{line}} T_{S} \tau_{H}(\mathbf{v}) d\mathbf{v} =$$

$$= 2.58 \cdot 10^{-15} N_{H} = T_{S} \tau_{H}$$

$$\tau_{H} = 2.58 \cdot 10^{-15} \frac{n_{H} I}{T_{s}} = 2.58 \cdot 10^{-15} \frac{N_{H}}{T_{s}}$$

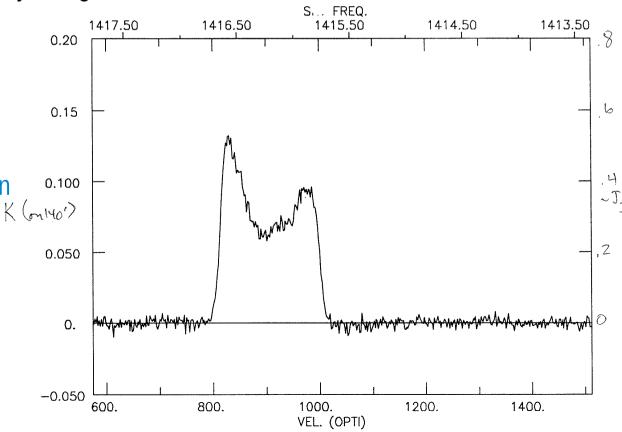


Observed 1.4 GHz radio image of the edge-on spiral galaxy NGC 891. All the continuum emission seen in the image comes from relativistic electrons (synchrotron continuum emission).

- > Hyperfine structure:  $\Delta E \sim 5.9 \mu eV$
- > Natural width of 21 cm line  $\sim 10^{-16}$  m/s

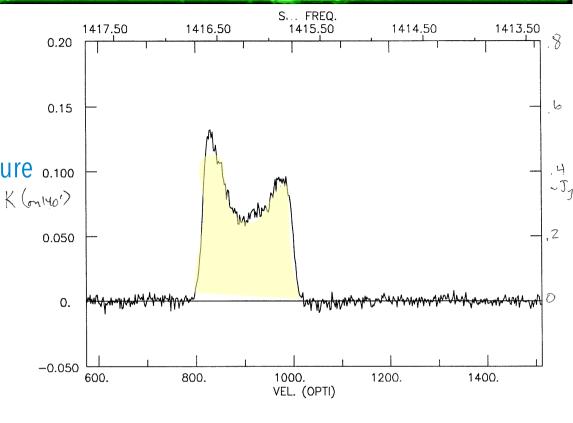
- Observed width ~100 km/s, up to 500 km/s in the Galactic centre
- a) Broadening due to the thermal motions of the gas
- b) Systematic shift due to radial velocity along the l.o.s:

Thermal/turbulent and/or systematic motions are studied using the 21 cm line, which has a gaussian profile (or superposition of clouds with Gaussian profiles and a distribution of radial velocities)

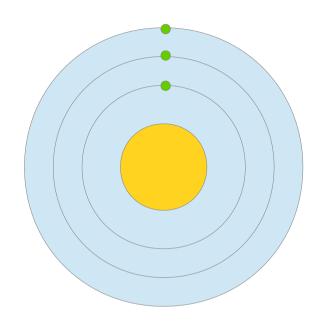


#### Neutral Hydrogen

- > Hyperfine structure:  $\Delta$ E ~ 5.9 μeV
- > Natural width of 21 cm line  $\sim 10^{-16}$  m/s
- The photons of the line are a direct measure 0.100 of the total amount of HI in the volume explored by the radio telescope
- In case of an optically thin emission



$$\frac{M}{M_{sun}} \approx 2.36 \cdot 10^5 \left(\frac{D}{Mpc}\right)^2 \int_{line} \left(\frac{S(v)}{Jy}\right) \left(\frac{dv}{km s^{-1}}\right)$$



#### **Differential rotation?**

♦ Let's assume circular orbits & same velocity

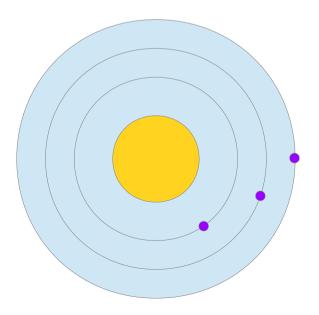
Inner regions have higher angular velocity (faster mix)

# Alternative options:

- Solid body rotation: constant angular velocity
- > **Keplerian decrease**: once the mass of the galaxy increases marginally with radius, such circular velocity should go with  $r^{-0.5}$ .

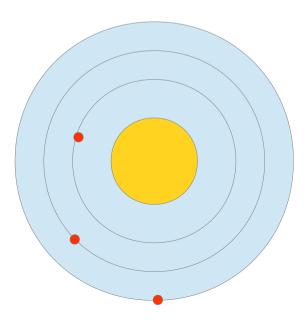
#### Differential rotation

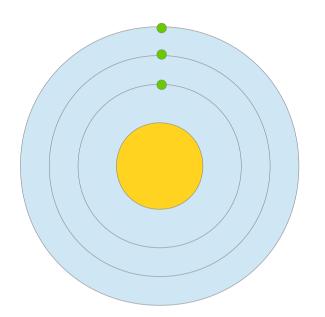
Time lapse 1: green points were aligned, purple points are not aligned anymore (each point has the same constant speed, but orbits with different lengths)



Differential rotation

Time lapse 2: red dots now appear uncorrelated



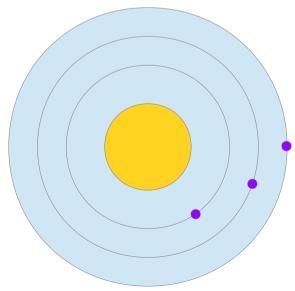


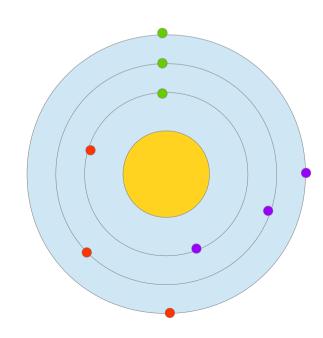
Differential rotation: **summary** 

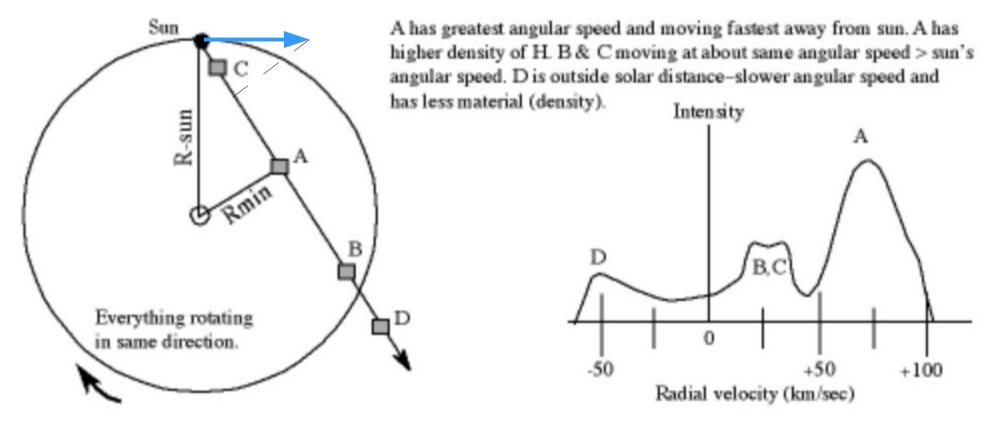
Green = stage 0, start

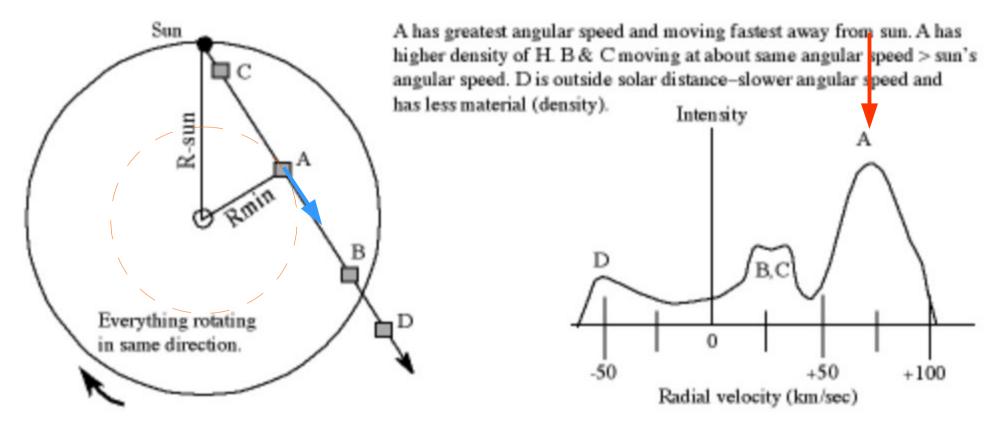
Purple = time lapse 1

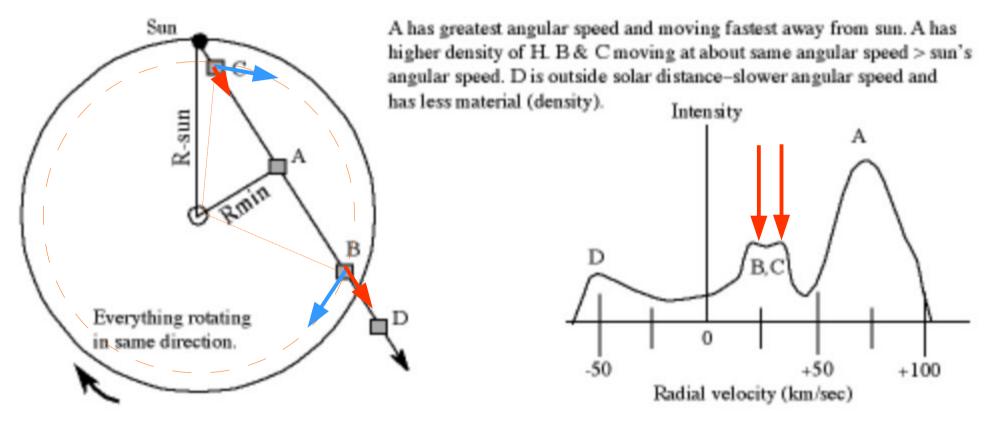
Red = time lapse 2

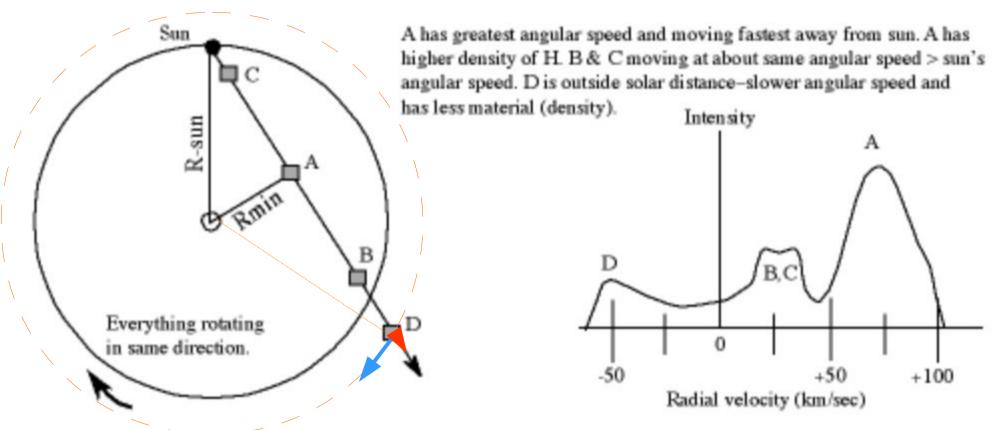




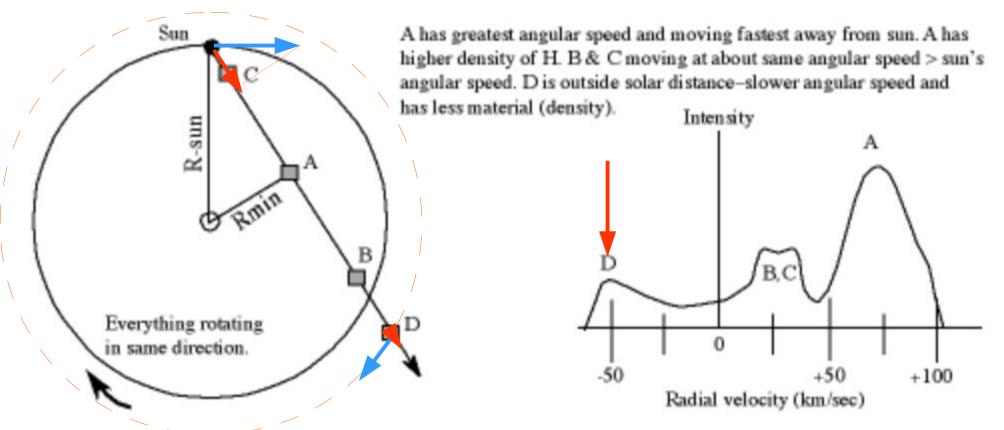








### Also the Sun moves, and has a component of the velocity along the line of sight!



#### Velocities within the MW

 $v_r$  must be computed along a given line of sight and has components from both  $\Omega_o R_o$  and  $\Omega R$ 

$$v_r = \Omega R \cos(\frac{\pi}{2} - L - \theta) - \Omega_o R_o \cos(\frac{\pi}{2} - L)$$

 $= \Omega R (\sin \theta \cos L + \cos \theta \sin L) - \Omega_o R_o \sin L$ 

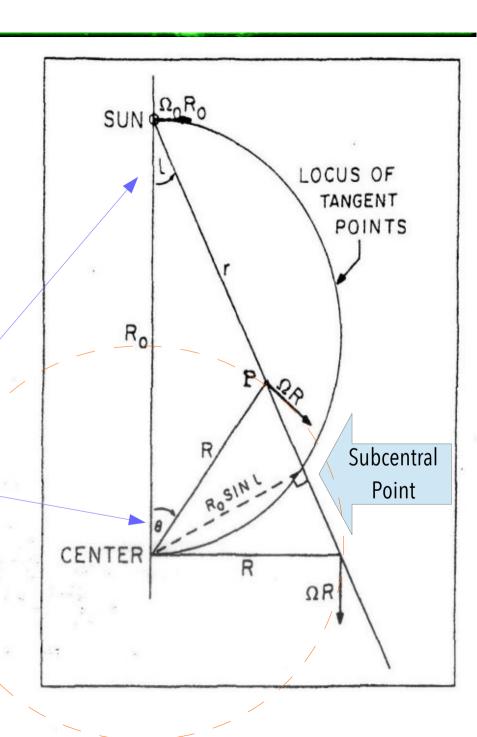
L is the galactic longitude (b is taken 0)

 $\theta$  is the galactocentric azimut

$$\frac{r}{\sin \theta} = \frac{R}{\sin L} \quad \text{i.e.} \quad r \sin L = R \sin \theta$$

$$R \cos \theta = R_o - r \cos L$$

$$v_r = R_o(\Omega(R) - \Omega_o) \sin L$$



Fundamental equation to determine the rotation curve (measuring the radial velocity)

$$v(R,L)_{r} = R_{o}(\Omega(R) - \Omega_{o}) \sin L$$

$$v(R,L)_{t} = R_{o}(\Omega(R) - \Omega_{o}) \cos L - r\Omega(R)$$

radial velocity tangential velocity

For a measured  $v_r$  in a given direction L, we can obtain  $\Omega(R)$ , from which the local circular velocity can be derived:  $v(R) = \Omega(R) \cdot R$ 

How to measure R: stars, HII regions, PN, ...? any distance indicator

In case R is not known and motions are axially symmetric to the GC (differential rotation)

Velocity has a maximum at the "sub-central" / "tangential" point

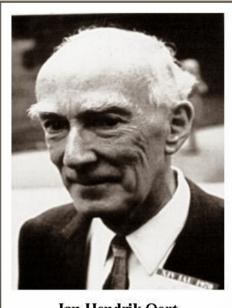
## Oort constants:

$$(\Omega(R) - \Omega_o)$$

Can be expanded in Taylor series to the first order and at the end we get

$$(\Omega(R) - \Omega_o) = \left(\frac{d\Omega}{dR}\right)_{R_o} (R - R_o) + \dots \quad \text{where } (R - R_o) \text{ is small}$$

$$\frac{d\Omega(R)}{dR} = \frac{d(v/R)}{dR} = \frac{1}{R} \frac{dv}{dR} - \frac{v}{R^2}$$



Jan Hendrik Oort 1900-1992

The radial velocity can be rewritten as

$$v_r = \left[ \left( \frac{dv}{dR} \right)_{R_o} - \frac{v_o}{R_o} \right] (R - R_o) \sin L = \left[ \frac{v_o}{R_o} - \left( \frac{dv}{dR} \right)_{R_o} \right] r \cos L \sin L$$

since in the solar neighborhood  $(R - R_o) \simeq r \cos L$ 

$$v_{r} = \frac{1}{2} \left[ \frac{v_{o}}{R_{o}} - \left( \frac{dv}{dR} \right)_{R_{o}} \right] r \sin 2L$$

first Oort constant: 
$$A = \frac{1}{2} \left[ \frac{v_o}{R_o} - \left( \frac{dv}{dR} \right)_{R_o} \right]$$
 allowing to write  $v_r = Ar \sin 2L$ 

The tangential velocity is 
$$v_t = \frac{v}{R}(R\cos L - r) - v_o\cos L = [\Omega(R) - \Omega_o]R\cos L - \Omega(R)r$$

using the same Taylor expansion

$$v_{t} = \left[\frac{v_{o}}{R_{o}} - \left(\frac{dv}{dR}\right)_{R_{o}}\right] r \cos^{2}L - \frac{v_{o}}{R_{o}} r = \left[\frac{v_{o}}{R_{o}} - \left(\frac{dv}{dR}\right)_{R_{o}}\right] \frac{r}{2} (1 \cos 2L) - \frac{v_{o}}{R_{o}} r$$

$$v_{t} = Ar \cos 2L - \left[\frac{v_{o}}{R_{o}} + \left(\frac{dv}{dR}\right)_{R_{o}}\right] \frac{r}{2}$$

defining the second Oort constant 
$$B = -\frac{1}{2} \left[ \frac{v_o}{R_o} + \left( \frac{dv}{dR} \right)_{R_o} \right]$$

The velocity of a given point at a distance r can be written as

$$v_r = A \cdot r \cdot \sin(2L)$$
  
 $v_t = A \cdot r \cdot \cos(2L) + B \cdot r$ 

with

$$A = \frac{1}{2} \left[ \frac{v_o}{R_o} - \left( \frac{dv}{dR} \right)_{R_o} \right]$$

$$B = -\frac{1}{2} \left[ \frac{v_o}{R_o} + \left( \frac{dv}{dR} \right)_{R_o} \right]$$

A and B are two coefficients dependent on R<sub>2</sub> and (d $\Omega$  / dR)<sub>2</sub>, known as Oort constants (1927)

$$A = \frac{1}{2} \left[ \frac{v_o}{R_o} - \left( \frac{dv}{dR} \right)_{R_o} \right]$$

$$B = -\frac{1}{2} \left[ \frac{v_o}{R_o} + \left( \frac{dv}{dR} \right)_{R_o} \right]$$

they can be computed by observations in the solar neighborhood.

> In case of a solid body rotation: 
$$A = 0$$
,  $B = -\Omega$ 

> In case of a solid body rotation: 
$$A = 0$$
,  $B = -\Omega_0$   
> In case of a Keplerian regime:  $A = 3/4 \text{ v}_0/R_0$ ,  $B = -1/4 \text{ v}_0/R_0$ 

Observed values

$$A = 14.82 \pm 0.84 \text{ km s}^{-1} \text{kpc}^{-1}$$
  
 $B = -12.37 \pm 0.64 \text{ km s}^{-1} \text{kpc}^{-1}$ 

Once known  $R_{\alpha} \sim 8.5$  kpc, the two constants allow to determine the velocity of the sun wrt the Galactic centre, v<sub>2</sub> ~220 km s<sup>-1</sup>

> In case of a solid body rotation: A = 0,

$$A = 0$$
,

$$B = - \Omega_{0}$$

$$\frac{dv}{dR} = \frac{v}{r} = \Omega$$

$$A = \frac{1}{2} \left[ \frac{v_o}{R_o} - (\Omega)_{R_o} \right] = \frac{1}{2} \left[ \frac{\Omega_o R_o}{R_o} - (\Omega)_{R_o} \right] = 0$$

$$B = -\frac{1}{2} \left[ \frac{v_o}{R_o} + (\Omega)_{R_o} \right] = -\frac{1}{2} \left[ \frac{\Omega_o R_o}{R_o} + (\Omega)_{R_o} \right] = -\Omega_o$$

> In case of a Keplerian regime: A=3/4 v/R, B=-1/4 v/R

$$A=3/4 v_o/R_o$$
,  $B=$ 

$$v = \sqrt{\frac{GM}{r}} \rightarrow \frac{dv}{dr} = -\frac{1}{2}\sqrt{\frac{GM}{r^3}} = -\frac{1}{2}\frac{v}{r}$$

$$A = \frac{1}{2}\left[\frac{v_o}{R_o} - \left(-\frac{v}{2r}\right)_{R_o}\right] = \frac{3}{4}\frac{v_o}{R_o}$$

$$B = -\frac{1}{2}\left[\frac{v_o}{R_o} + \left(-\frac{v}{2r}\right)_{R_o}\right] = -\frac{1}{4}\frac{v_o}{R_o}$$

> In case of a flat rotation curve:

$$A=1/2 v_{o}/R_{o}$$
,

$$\frac{dv}{dr} = 0$$

$$A = \frac{1}{2} \left[ \frac{v_o}{R_o} - (0)_{R_o} \right] = \frac{1}{2} \frac{v_o}{R_o}$$

$$B = -\frac{1}{2} \left[ \frac{v_o}{R_o} + (0)_{R_o} \right] = -\frac{1}{2} \frac{v_o}{R_o}$$

$$\left( \frac{dv}{dr} \right)_{R_o} = -A - B = -3.4 \, \text{km s}^{-1}$$

$$A = 14.82 \pm 0.84 \, \text{km s}^{-1} \, \text{kpc}^{-1}$$

$$B = -12.37 \pm 0.64 \, \text{km s}^{-1} \, \text{kpc}^{-1}$$

Since A  $\sim$  – B, the rotation curve derived for out galaxy is ~ flat

$$A=1/2 \text{ v}/R_0$$
,  $B=-1/2 \text{ v}/R_0$ 

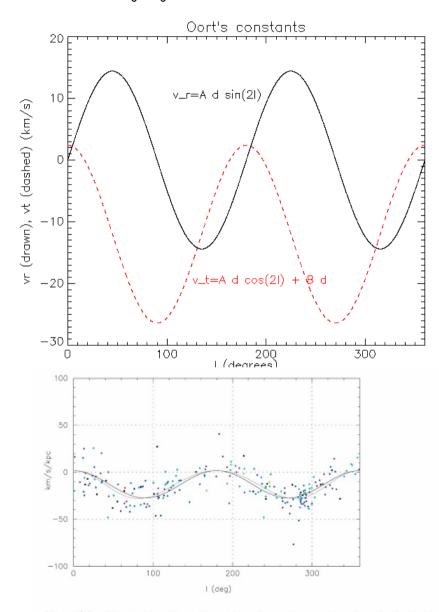
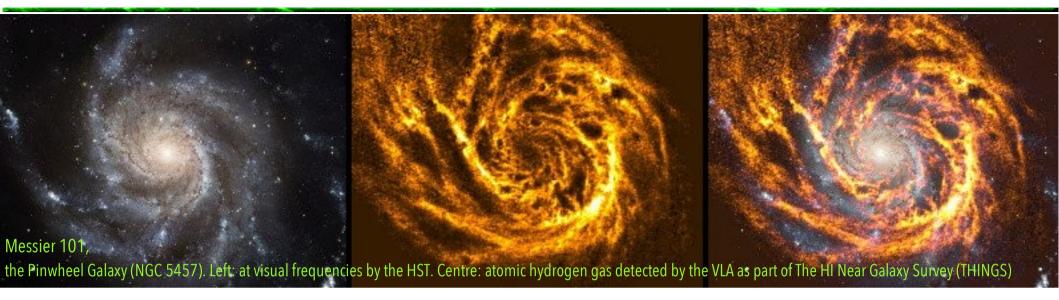
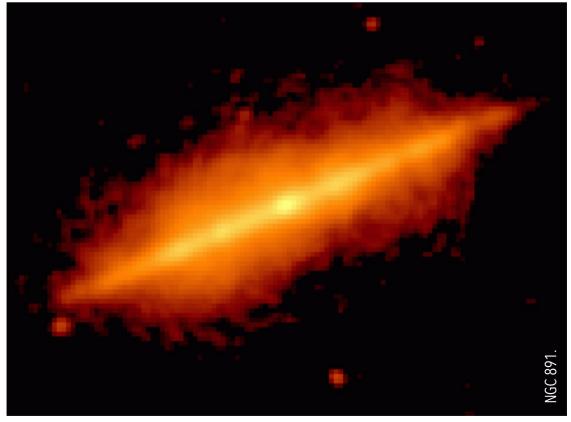


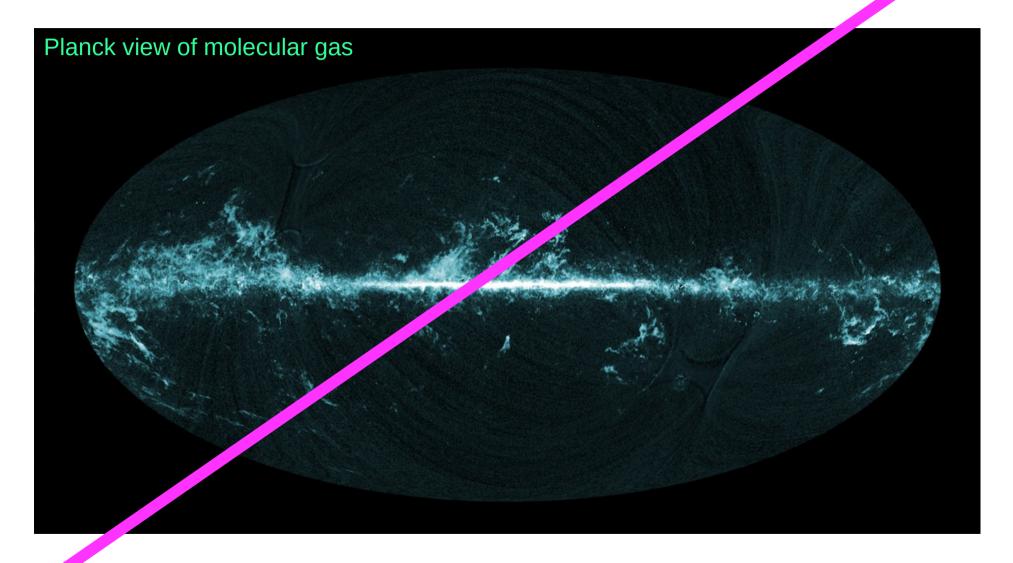
Figure 6.6. The quantity  $\kappa \mu_l$ , corrected for solar motion, as a function of galactic longitude, showing the effect of galactic rotation. The solid curve shows the fitting of the data for stars within 1 kpc from the Sun, the grey curve shows the same for stars with a projected distance of 5 kpc. Only stars with projected distances beyond 1.2 kpc are shown and used in the solution for the curves shown here

## Rotation curve: going out to external galaxies

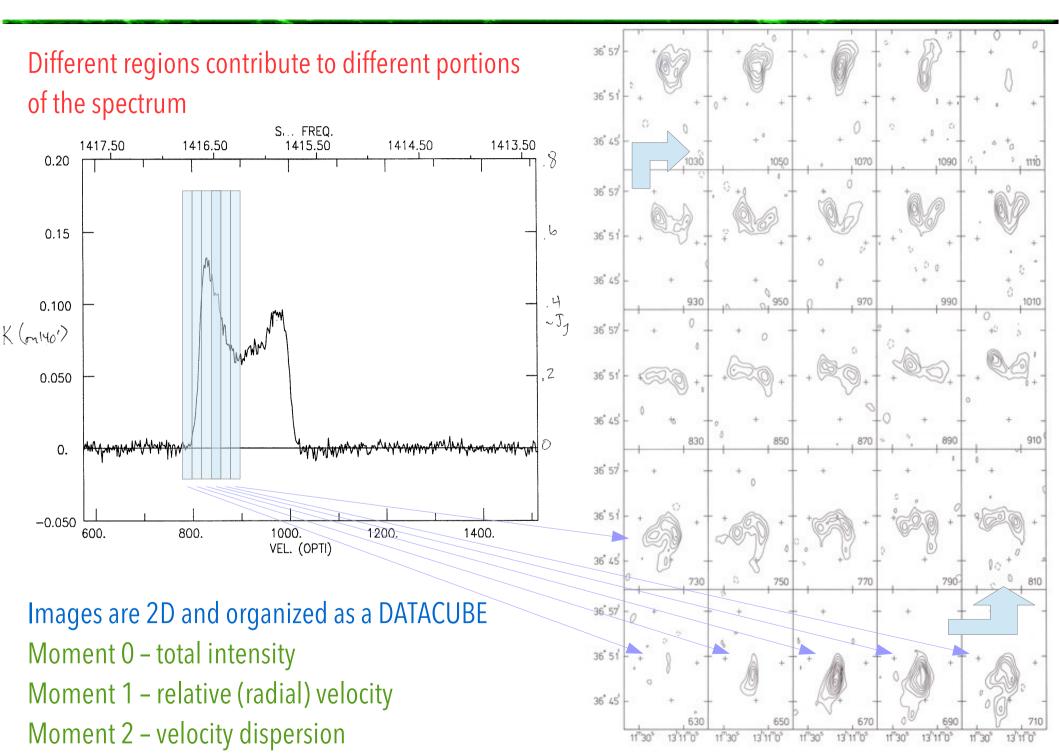


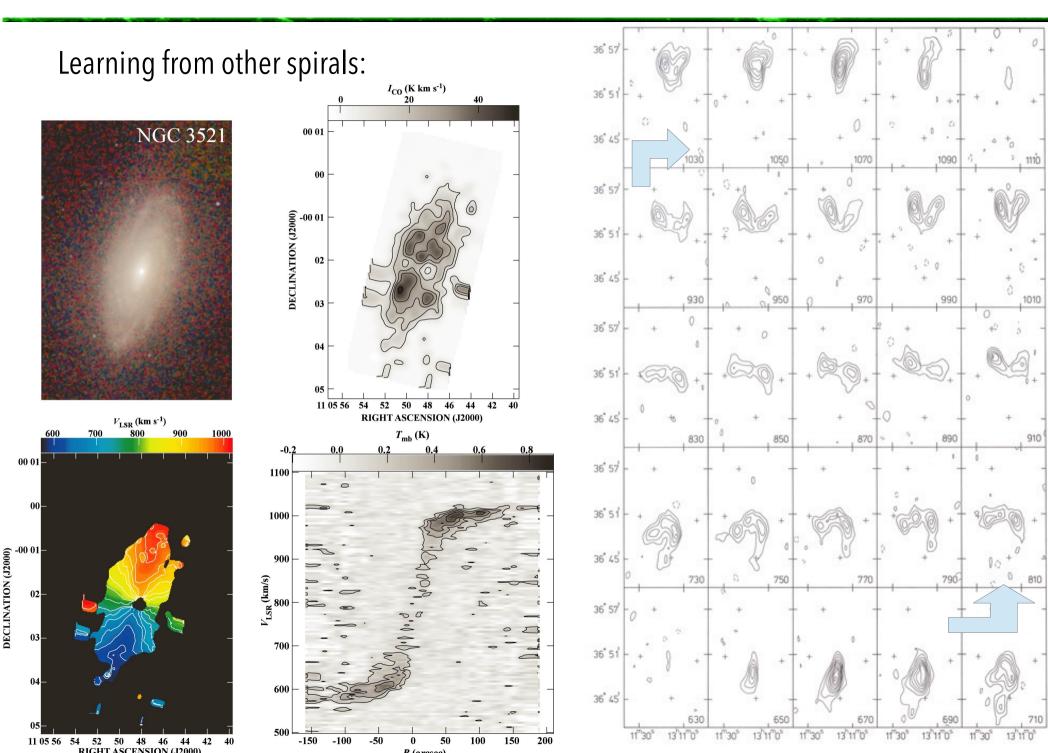


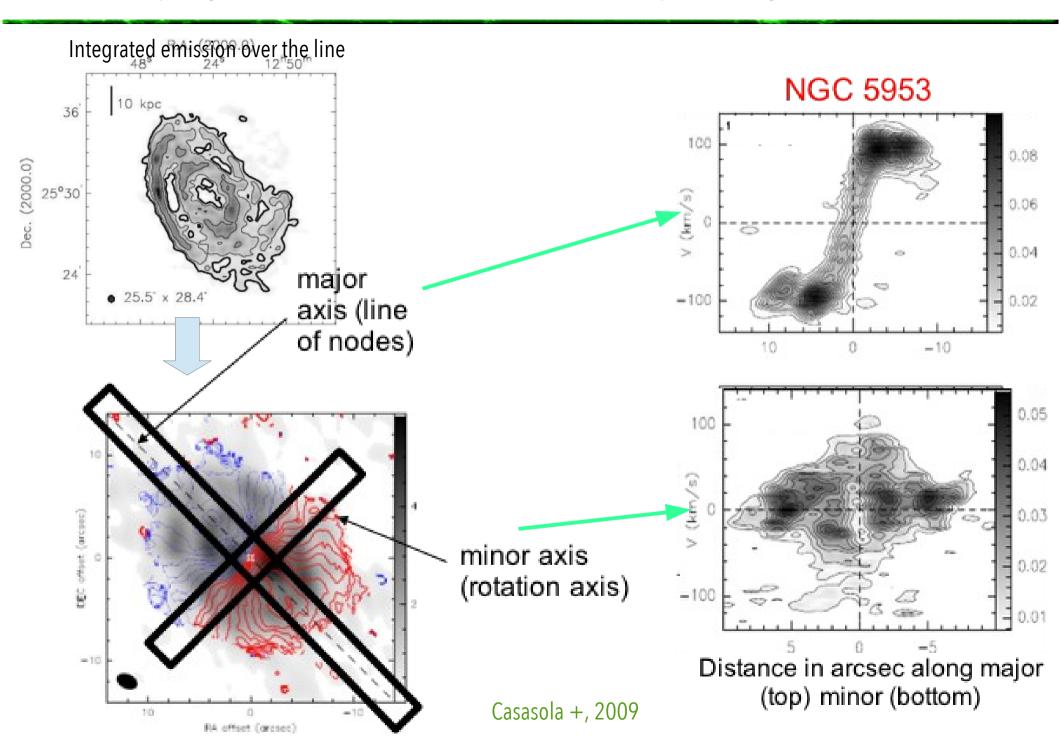
CO: also the molecular gas can be used to trace both distribution and dynamics



Zocated in different regions, is an independent tracer of the galactic dynamics In particular, very important in SFG and SBG. Complete analogy to HI line analysis







#### The PV diagram: interpretation

PV diagram

Simulations of beam-smearing on a major-axis PV diagram.

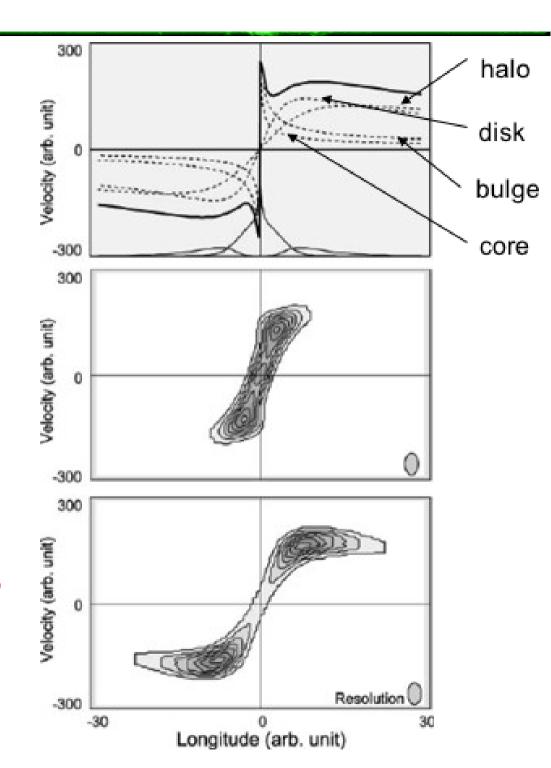
Top: Assumed "true" rotation curve (thick) with a central core, bulge, disk, and halo

Middle: "Observed" CO PV diagram

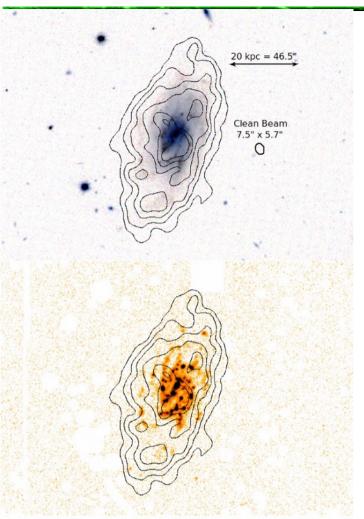
Bottom: "Observed" HI PV diagram

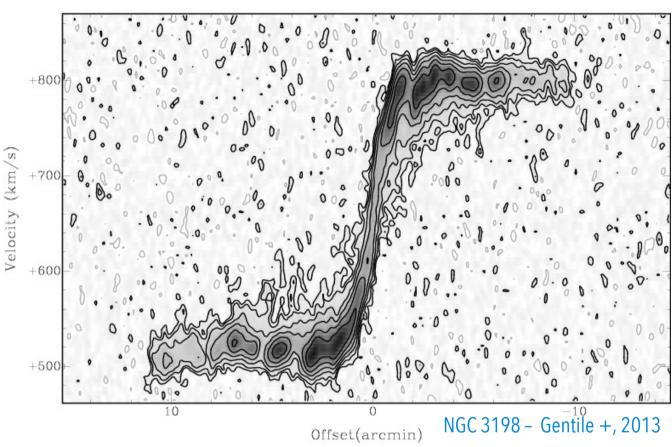
High resolution & high sensitivity necessary to detect central high velocities and steep rise

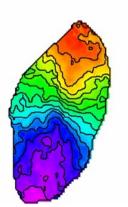
(Sofue & Rubin 2001)



#### HI in external galaxies Galaxies ==> ricollocare







Contours: total HI emission;

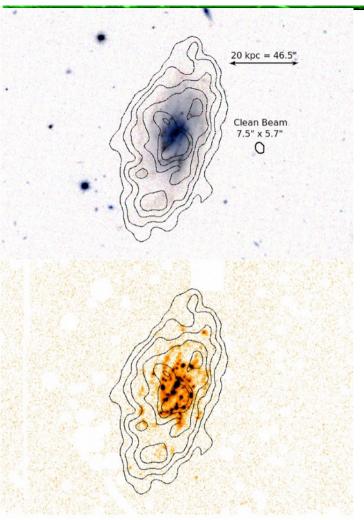
Top: optical from SDSS

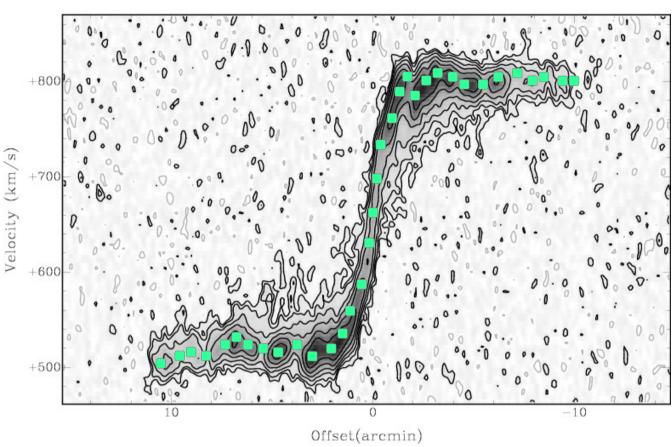
Middle:  $H\alpha$ , from Huang+, 2014

Bottom: HI velocity field from ALFAALFA

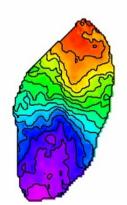
Hallenbeck +, 2014

#### HI in external galaxies Galaxies





Turquoise points define the rotation curve (on both sides!)



Contours: total HI emission;

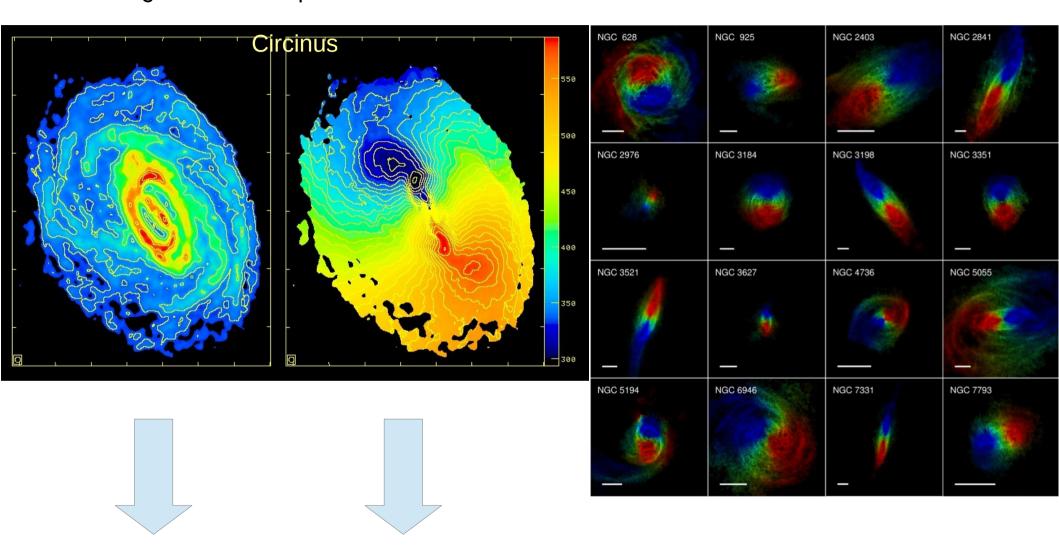
Top: optical from SDSS

Middle:  $H\alpha$ , from Huang + 2014

Bottom: HI velocity field from ALFAALFA

Hallenbeck +, 2014

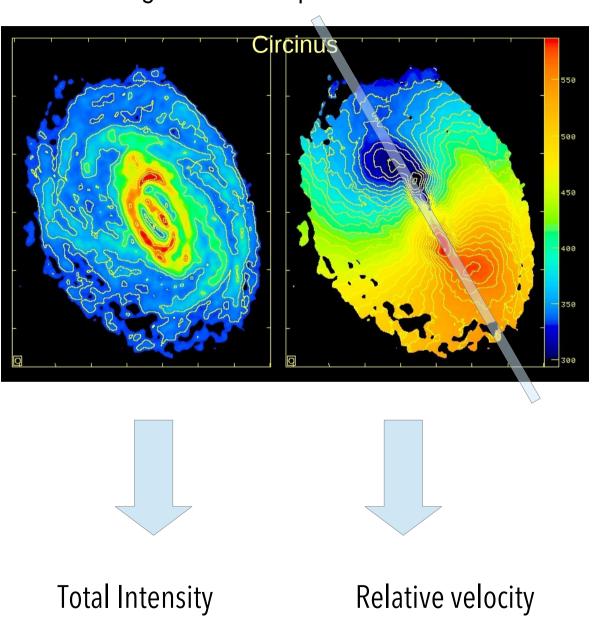
# Learning from other spirals:



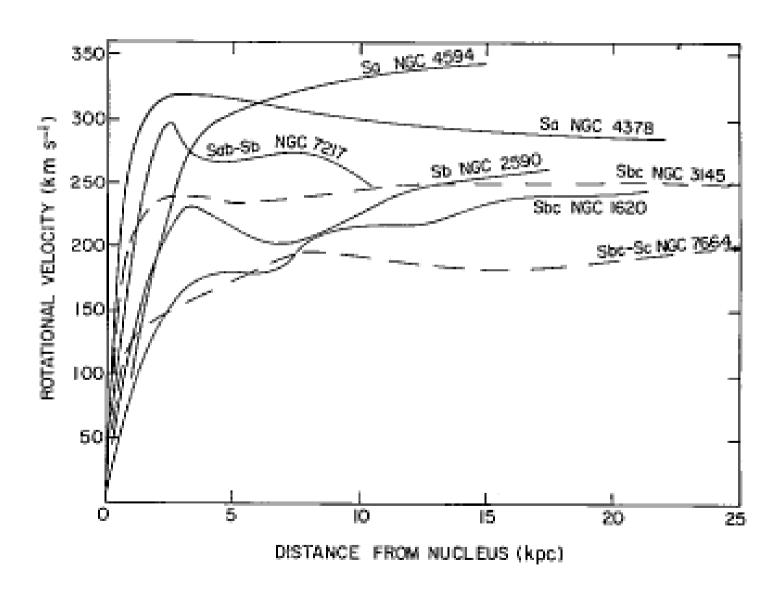
**Total Intensity** 

Relative velocity

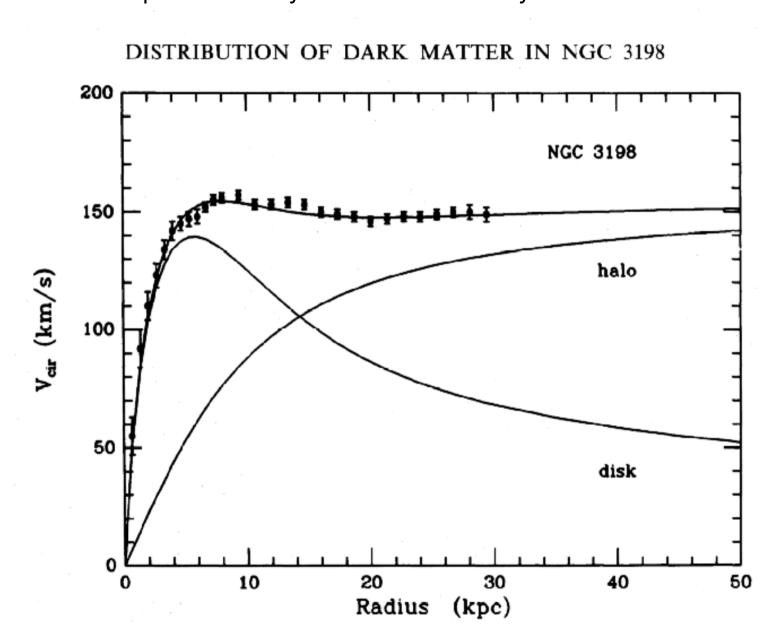
# Learning from other spirals:



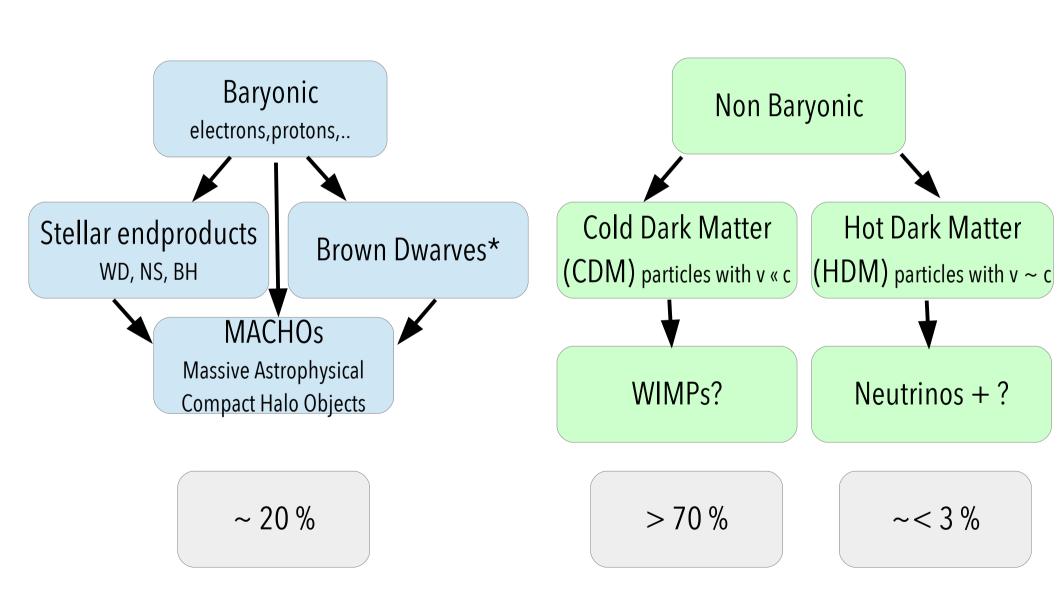
### Observations:



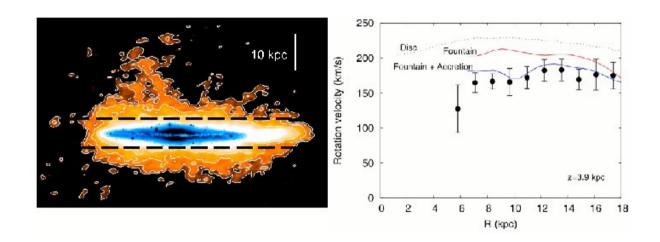
Observations: the "keplerian" decay of the radial velocity is never observed: Dark MATTER!

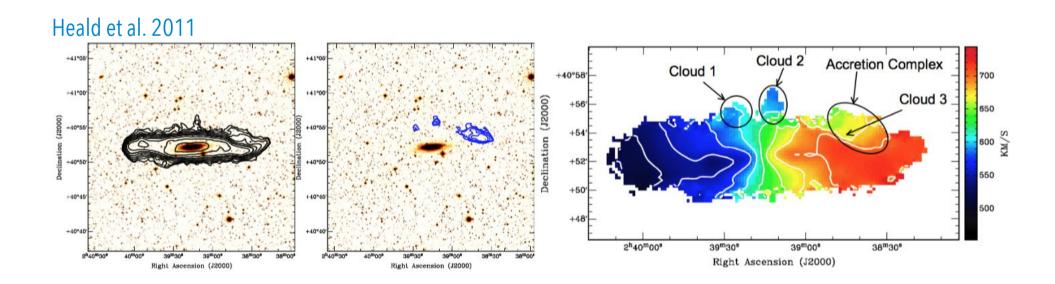


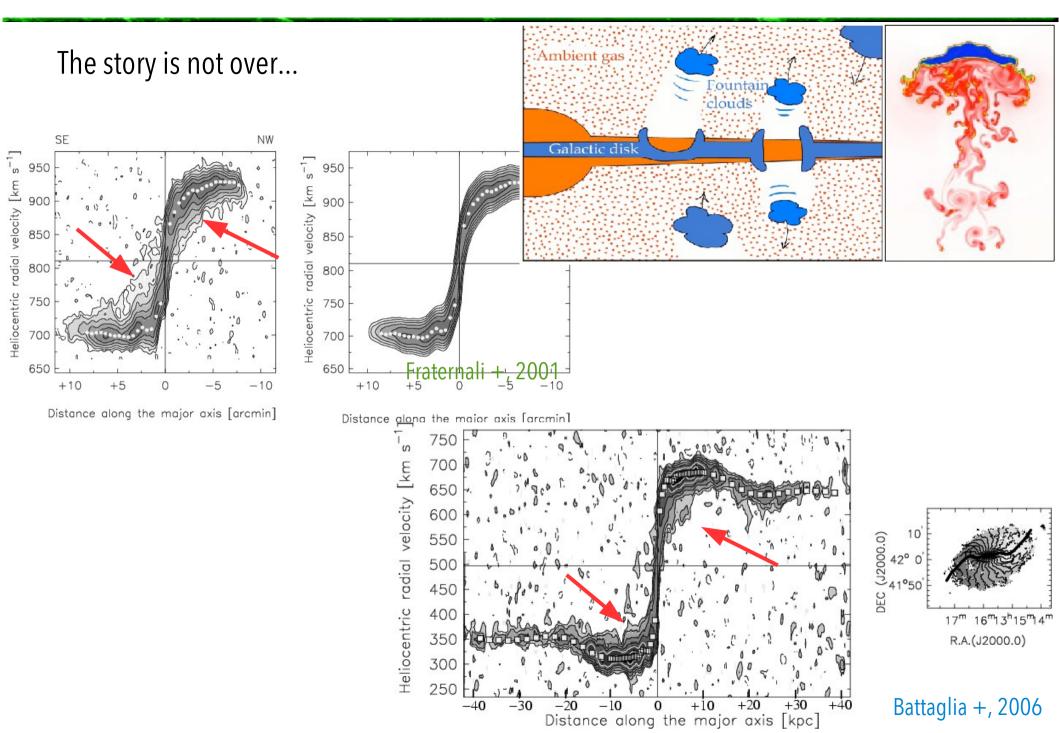
#### Constraints on Dark Matter:



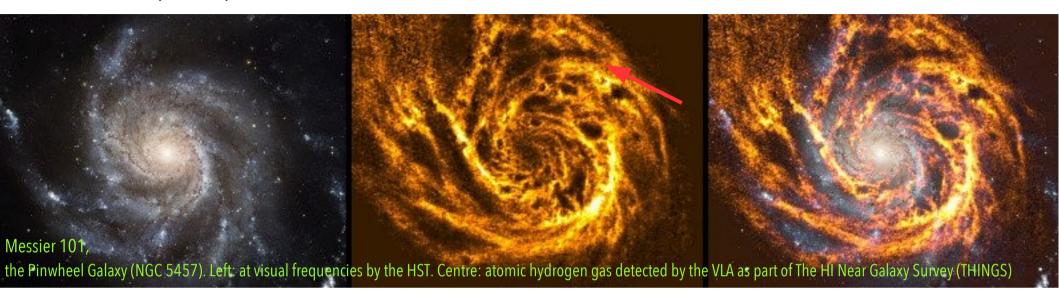
# The story is not over... **extra-planar clouds**

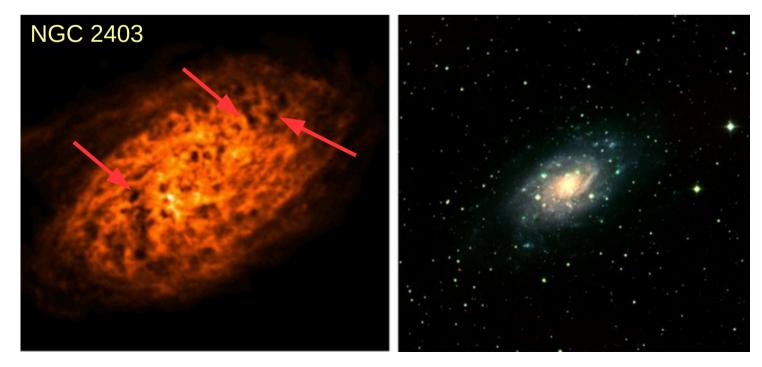


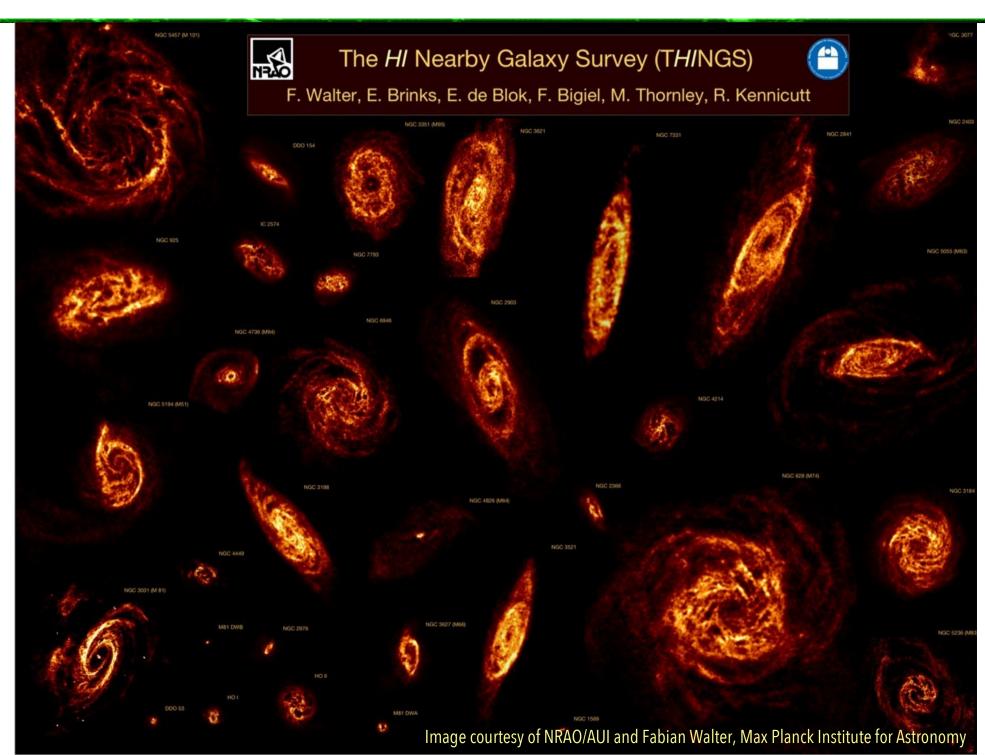




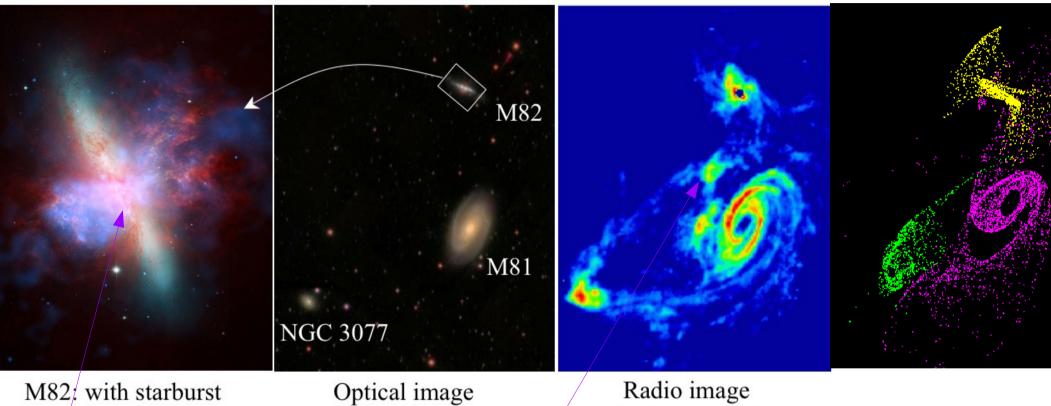
# Bubbles (holes) in HI distribution







Groups
Interaction triggers starburst and outflow in M82

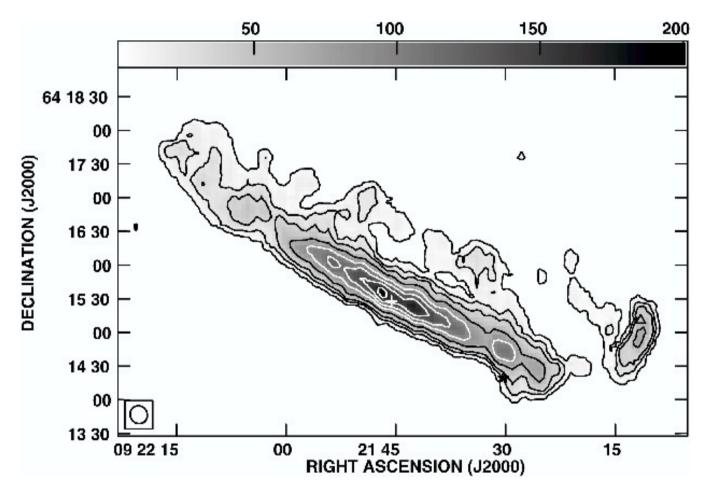


- M82: with starburst driven outflowing wind
- Optical image (starlight)

Radio image (hydrogen gas)

- Tidal interaction (physical link)
- Different dynamical times: gas/stars
- Induced star formation
- Gas concentrations also in "empty parts of the sky"

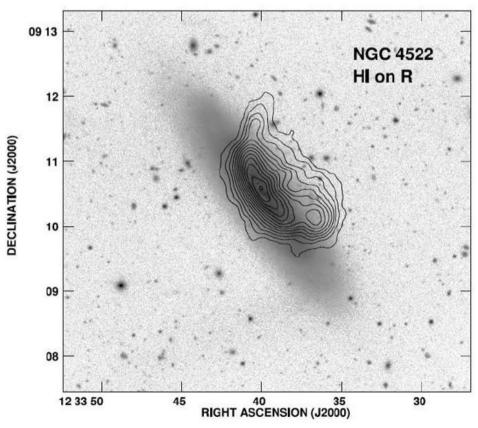
# Lopesidedness



- > Environment weather
- Galaxy motion

# Galaxy clusters

- HI deficiency
- Morphological segregation



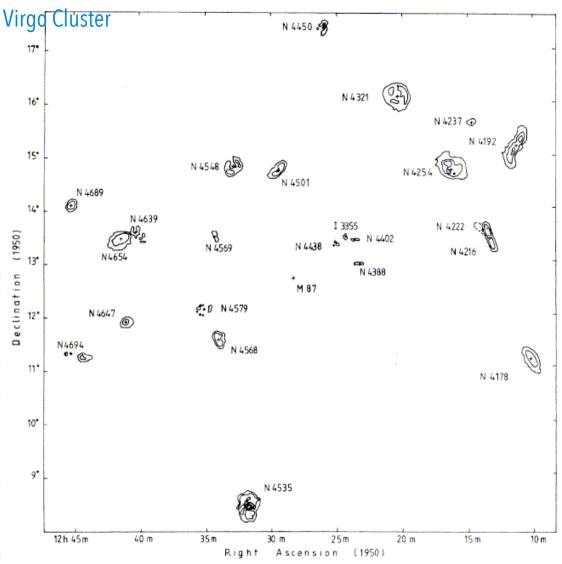


Fig. 23. Integrated neutral hydrogen maps of the brightest spirals in the Virgo Cluster center. Each map has been drawn at the galaxy position indicated by a cross and magnified by a factor of 5 compared with the scale in right ascension and declination. The first contour in each map corresponds approximately to a column density of 10<sup>20</sup> atoms cm<sup>-2</sup> (even if it is not the case in the maps published in Figs. 1–22 especially for NGC 4388, 4450, 4569, 4694).

Ram pressure stripping

### Summary

- > In spirals HI is distributed on a large fraction of the volume
- > HI traces the neutral & warm ISM
- Line emission (absorption) very effective kinematic tool
- Rotation curve & Oort constants
- Dark matter
- External spirals
- Neutral gas effects (e.g. Lopesidedness, extra-planar gas, bubbles, etc)

- Suggested readings:
- Fanti & Fanti , § 13
- Tools of Radio Astronomy, , § 13

# Galactic and Extragalactic Magnetic Fields



- > Stars
- > Pulsars
- > SNR
- Microquasars
- > ISM
- The GC, SgrA\*
- Normal Galaxies
- · Elliptical, Spirals
- AGN &Radio sources
- Compact/Extended, core, jets, lobes/tails
- > IGM
- · Clusters of galaxies, filaments, etc.



# Probes for astrophysical H field

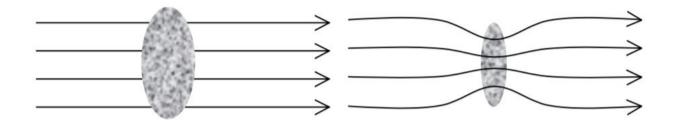
- Synchrotron emission
- Polarization
- Faraday Rotation
- Zeeman Effect
- Cosmic Rays in the Milky Way
- Starlight polarization & polarized Dust emission
- Circular polarization in Masers

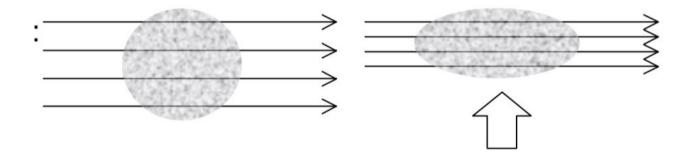


- flux freezing in plasma
- energy budget in the ISM
- strong influence on star formation
- confinement and acceleration of cosmic rays



- flux freezing in plasma (amplification)







### - energy budget in the ISM

Thermal gas pressure 
$$P_{therm} \approx 0.3 10^{-12} dyn cm^{-2}$$

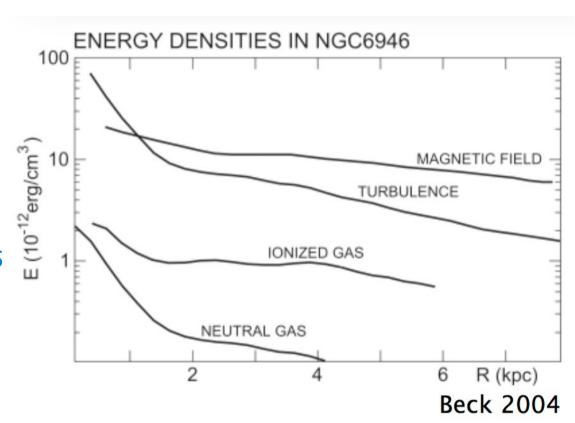
Magnetic pressure 
$$P_{H} = H^{2}/8\pi \approx (0.4 - 1.4) \quad 10^{-12} \text{ dyn cm}^{-2}$$

Cosmic ray pressure 
$$P_{CR} \approx (0.8 - 1.6) 10^{-12} \text{ dyn cm}^{-2}$$

Turbulent gas pressure 
$$P_{turb} \approx \rho \sigma^2 \approx (1.0 - 1.5) \ 10^{-12} \, dyn \, cm^{-2}$$

Boulares & Cox 1990

Energy densities in magnetic fields, cosmic rays, and turbulent gas are comparable in the ISM, on large scales





- strong influence on star formation

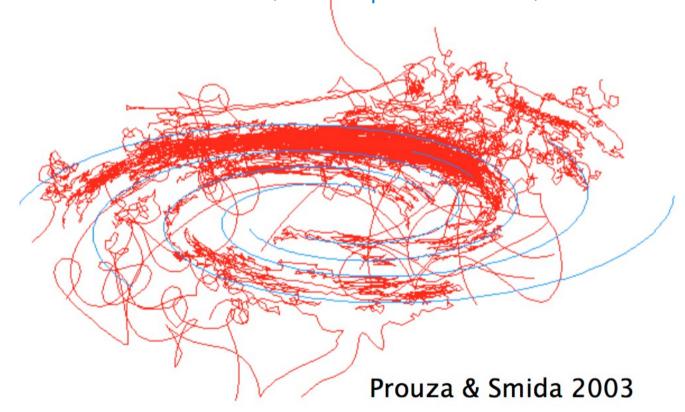
#### H:

- provides support against gravitational collapse through flux freezing u delays collapse
- transport angular momentum away from collapsing protostellar cores ("magnetic braking") u enhances collapse
- reduces heat conduction significantly u cloud evaporates much slower, and can be further compressed u enhances collapse



- confinement and acceleration of cosmic rays
- CRs are deflected by galactic H, directions are randomized
- Confinement for about 10 Myr

• Generated/accelerated in SNR and shocks (field amplification του:)



# Probes for astrophysical H field

- Synchrotron emission
- Polarization
- Faraday Rotation
- Zeeman Effect
- Cosmic Rays in the Milky Way

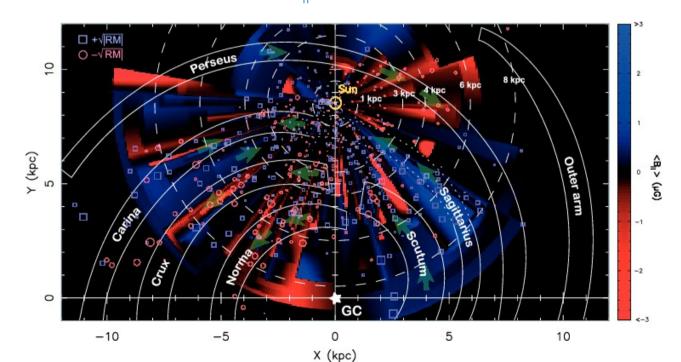
# Probes for astrophysical H fields

- From synchrotron emission lis the depth of the source

$$B(\mathbf{v}) \simeq NH^{(\delta+1)/2}I$$
 where  $N=N_{\alpha}\varepsilon^{-\delta}$ 

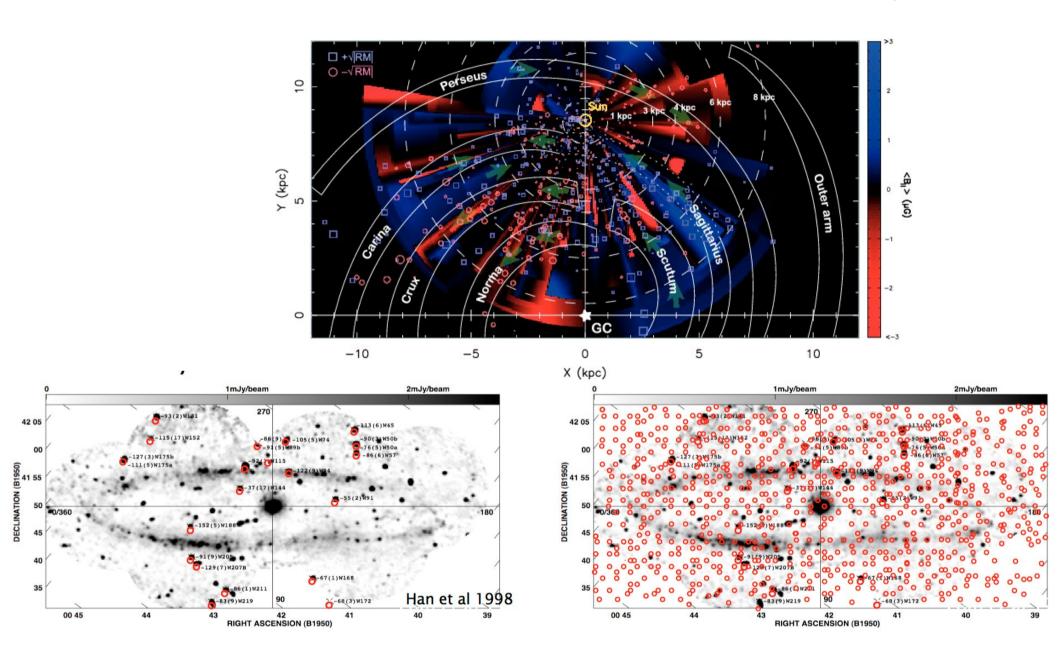
### Our galaxy:

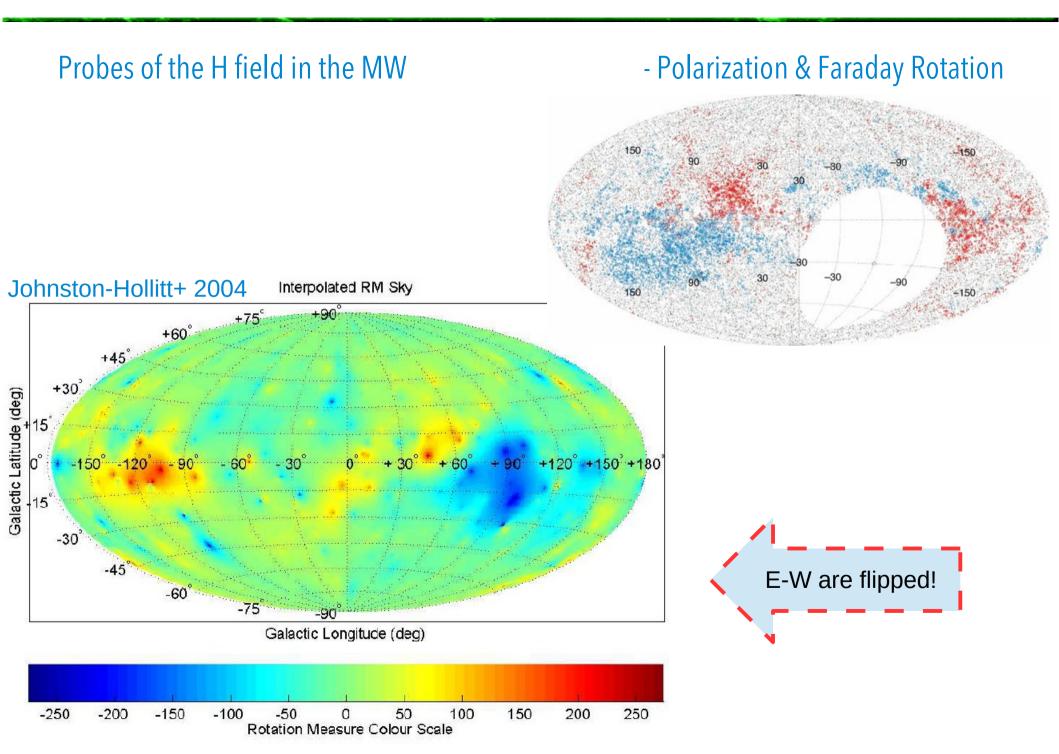
- if N $_{_{0}} \sim 0.01$  cm  $^{\text{-}3}$  as found in the solar neighborhood  $\implies$  H  $\sim 10 \mu G$
- Pulsar <RM> / <DM>  $\implies$  H  $_{\parallel}$   $\sim$  5-6  $\mu$ G



#### Probes of the H field in the MW

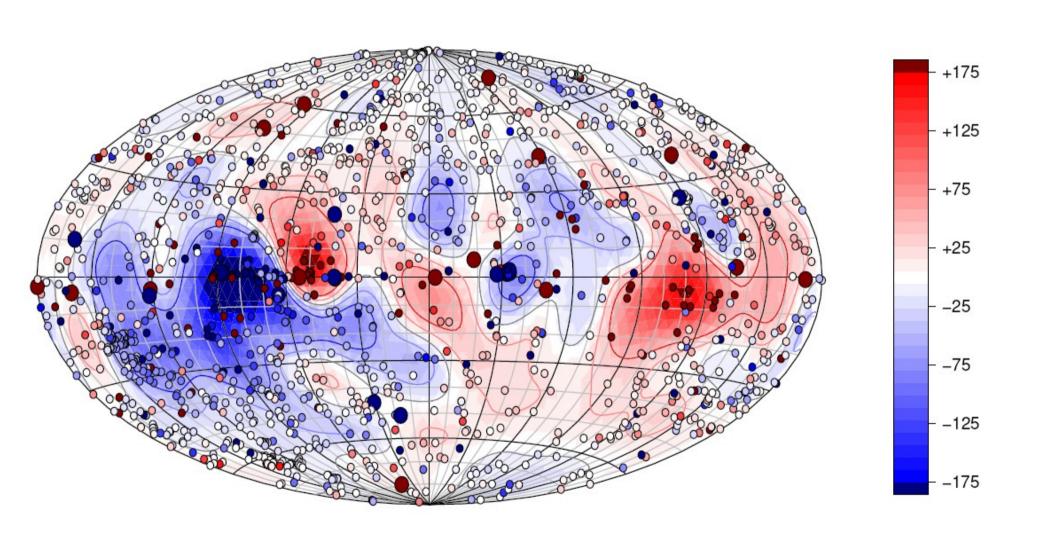
# - Polarization & Faraday Rotation





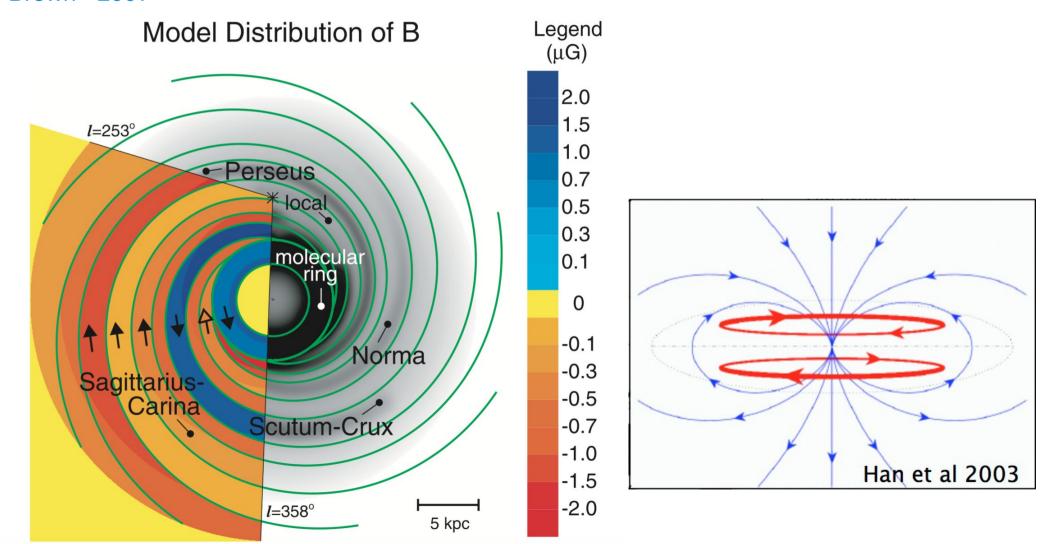
### Probes of the H field in the MW

# - Polarization & Faraday Rotation



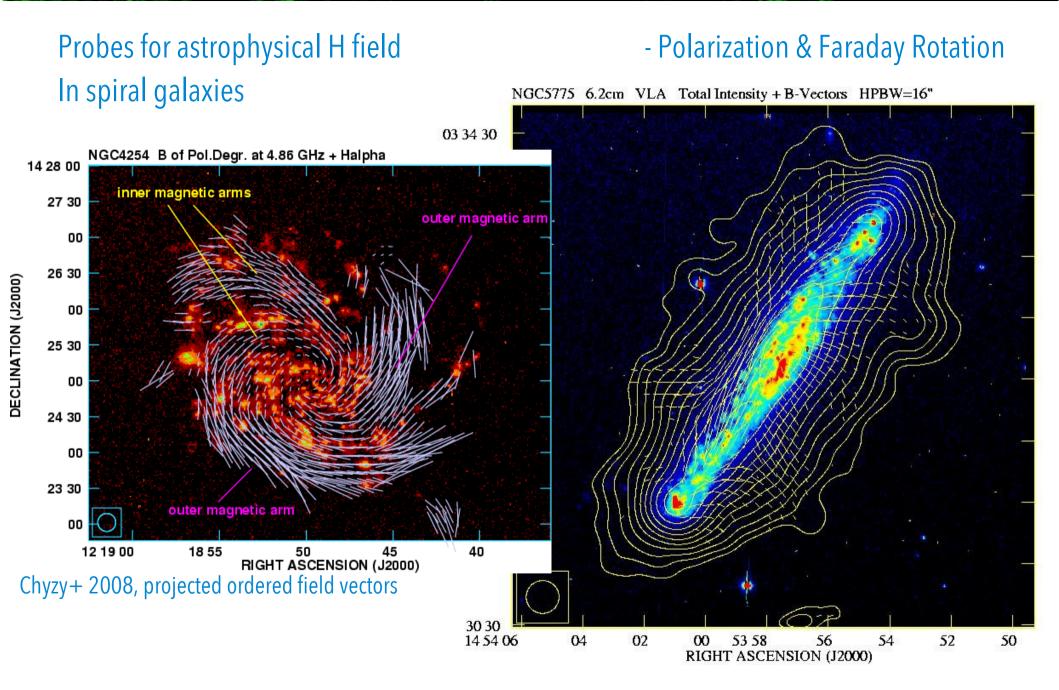
Probes of the H field in the MW - Polarization & Faraday Rotation Model(s) for the field in the Milky Way Field Reversals

#### Brown+ 2007



# Nearby external galaxies

- > Halos are seen around disks of many edge-on spirals.
- Radio intensity and halo extent vary greatly
- > There is a rough correlation with Há and X-rays: star formation in the disk is an energy source for halo formation



Tullmann + 2000, projected ordered field vectors

Probes for astrophysical H field Spirals:

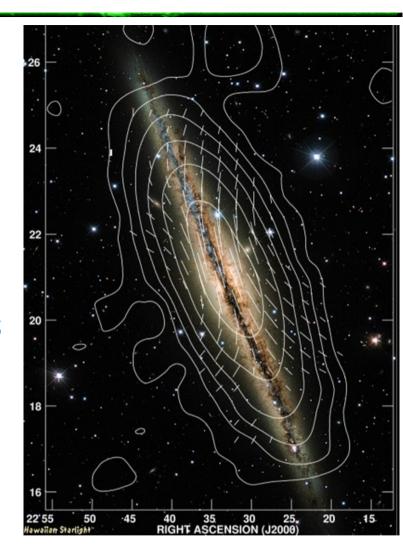
 $B \approx 10 \, \tilde{O}G$  in typical spirals (M31, M33);

 $B \approx 15 \, \tilde{O}G$  for high-star forming galaxies (M51)

 $B \approx 30 \, \tilde{O}G$  for starburst galaxies (M82, Antennae)

B<sub>uniform</sub> is usually the strongest in the inter-arm regions

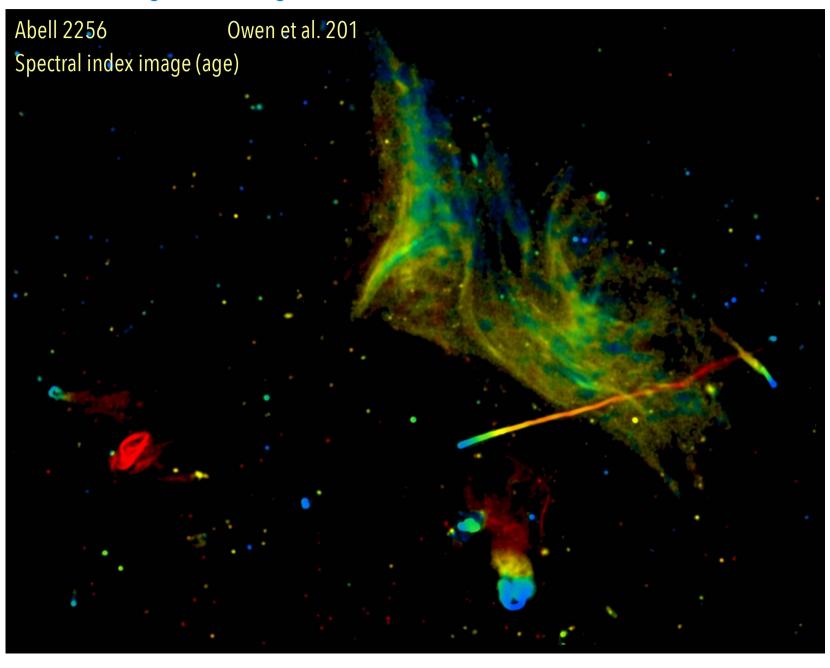
Spiral magnetic field exists in almost all galaxies, even the ringed and flocculent ones! This is a strong indication of dynamo action in these galaxies, that maintains a (spiral) magnetic field in these galaxies



# **Intergalactic magnetic fields**

- "Empty" space (VOIDs) may be magnetized.
   It may provide a seed field for galaxy and cluster magnetic fields.
   What role do intergalactic magnetic fields have in structure formation in the early Universe?
- ⇒ Upper limit from Faraday rotation observations:  $B_{IGM} \le 10^{-8} 10^{-9}$  Gauss Similar to upper limits from many theoretical studies
- In Galaxy Clusters
- $B_{IGM} \sim 10^{-6} 10^{-7}$  Gauss (from RM of background sources, and extended radio sources within the cluster) Some fraction (mostly the X-ray bright & most massive ones, morphologically disturbed) have diffuse radio emission.
- Origin of cluster magnetic fields:
   outflows from AGNs, turbulent wakes, cluster mergers etc.

# Cluster scale intergalactic magnetic fields



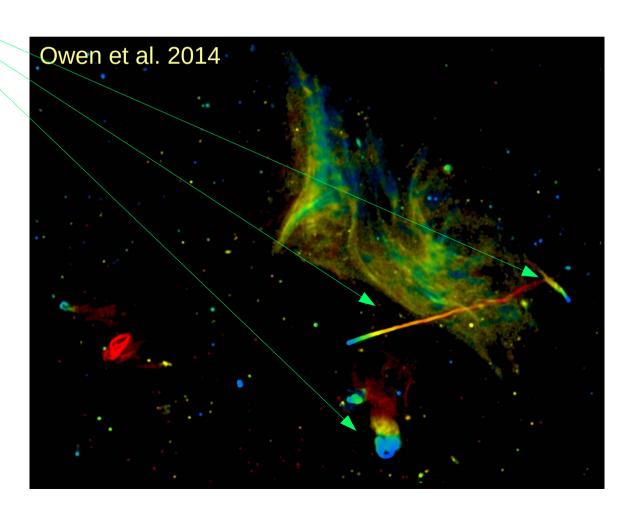
Synchrotron emission (relativistic electrons, H)

> Spectral ageing in tailed radio galaxies (2D speed, evolution of H &  $\gamma$  in the tails, pressure

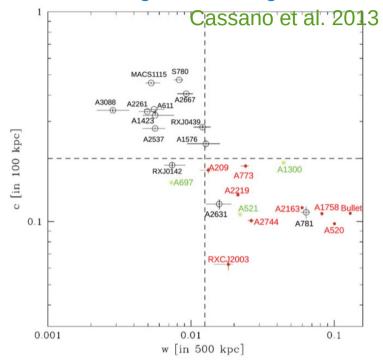
equilibrium with the IGM)

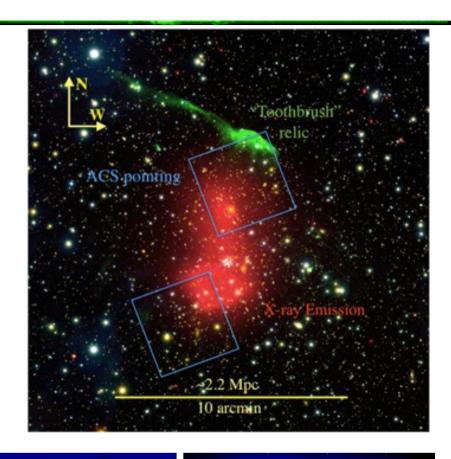
RM in extended emission (2D tomography of the H field and n<sub>e</sub> along various LOS)

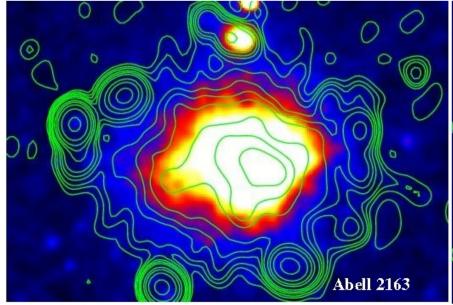
Energy content in relativistic plasma
 & energy budget of the ICM

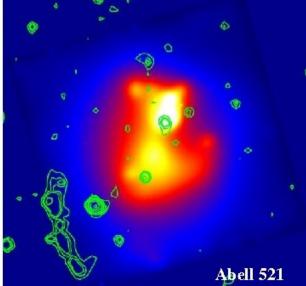


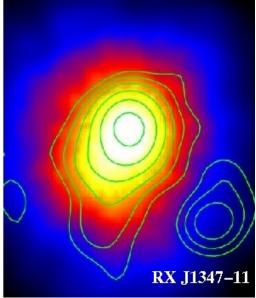
# Cluster scale intergalactic magnetic fields





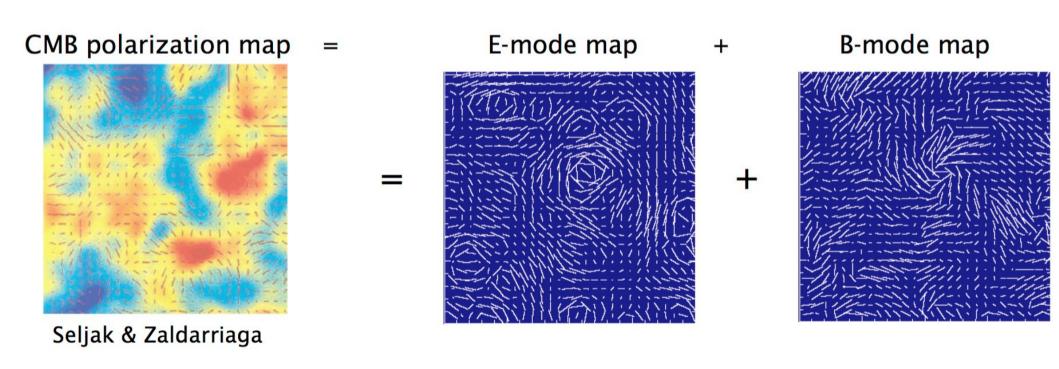




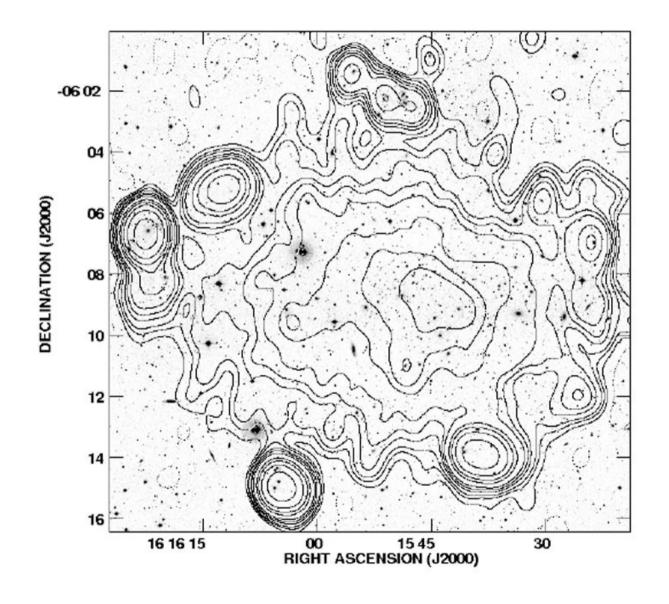


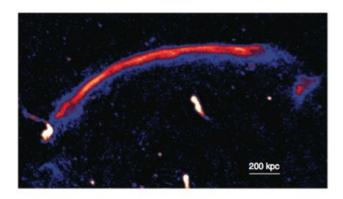
### CMB linear polarisation can be decomposed into E-modes and B- modes

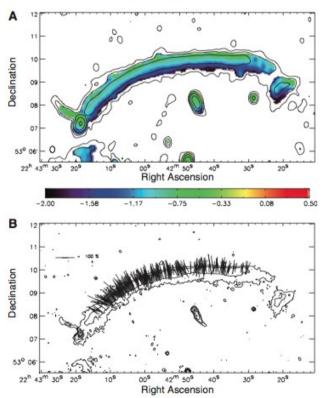
- -- similar to decomposition in Stokes Q, U but without a preferred coordinate system. (In effect the E-mode is a curl-free mode, while the B-mode is divergence-free.)
- ⇒ E-modes arise from Thomson scattering in an inhomogeneous plasma
- ⇒ B-modes determined by primordial gravitational wave density t signal from inflation era!



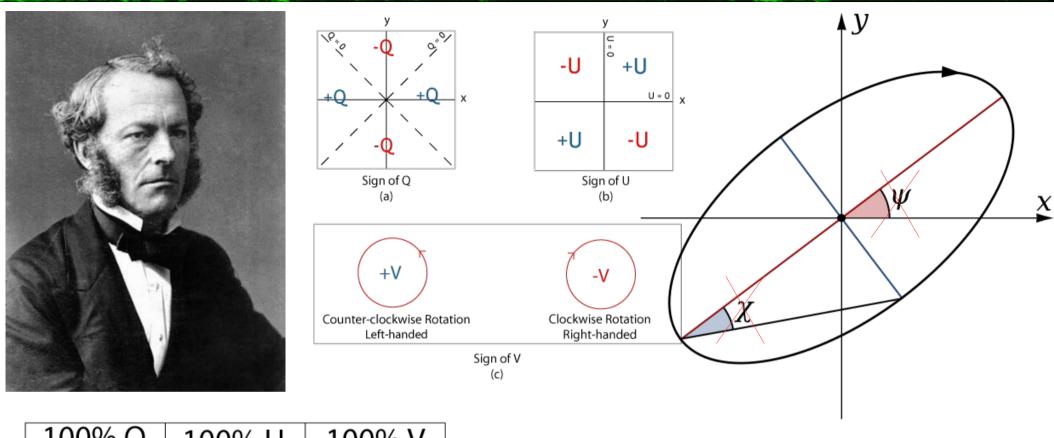
### Much more in the "AMMASSI DI GALASSIE" lectures



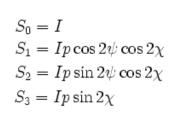


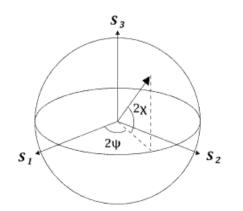


#### Appendix: linear, circular polarization and the Stokes' Parameters



100% Q	100% U	100% V	
+Q   y	+U   <sup>y</sup>	+V y	
х	45° X	x	
Q > 0; U = 0; V = 0 (a)	Q = 0; U > 0; V = 0 (c)	Q = 0; U = 0; V > 0 (e)	
-Q	-Ų  y	-V y	
x	45 x	×	
Q < 0; U = 0; V = 0 (b)	Q = 0, U < 0, V = 0 (d)	Q = 0; U = 0; V < 0 (f)	





- 2. Parametrization of the linear (and circular) polarization: Stokes' Parameters Each radio telescope reveals two orthogonal components of the radiation
- a. linear feeds  $E_x$ ,  $E_y$
- b. circular feeds  $E_R$ ,  $E_L$

Both interferometers and single dishes cross (auto) correlate these signals

$$\langle E_{\chi}^{2} \rangle + \langle E_{\gamma}^{2} \rangle = I$$

$$\langle E_{\chi}^{2} \rangle - \langle E_{\gamma}^{2} \rangle = Q$$

$$2 \langle \text{Re}(E_{\chi} E_{\gamma}^{*}) \rangle = 2 \langle \text{Re}(E_{\chi} E_{\gamma}) \cos \delta_{\chi \gamma} \rangle = U$$

$$2 \langle \text{Im}(E_{\chi} E_{\gamma}^{*}) \rangle = 2 \langle \text{Im}(E_{\chi} E_{\gamma}) \sin \delta_{\chi \gamma} \rangle = V$$

$$I = \langle E_R^2 \rangle + \langle E_L^2 \rangle$$

$$Q = 2 \langle \text{Re}(E_R E_L^*) \rangle = 2 \langle \text{Re}(E_R E_L) \cos \delta_{RL} \rangle$$

$$U = 2 \langle \text{Im}(E_R E_L^*) \rangle = 2 \langle \text{Im}(E_R E_L) \sin \delta_{RL} \rangle$$

$$V = \langle E_R^2 \rangle - \langle E_L^2 \rangle$$

2. Relationships for an interferometer: given two antennas i- and j- with circular feeds:

$$I = \frac{(E_R^i E_R^j + E_L^i E_L^i)}{2}$$

$$Q = \frac{(E_R^i E_L^j + E_L^i E_R^j)}{2}$$

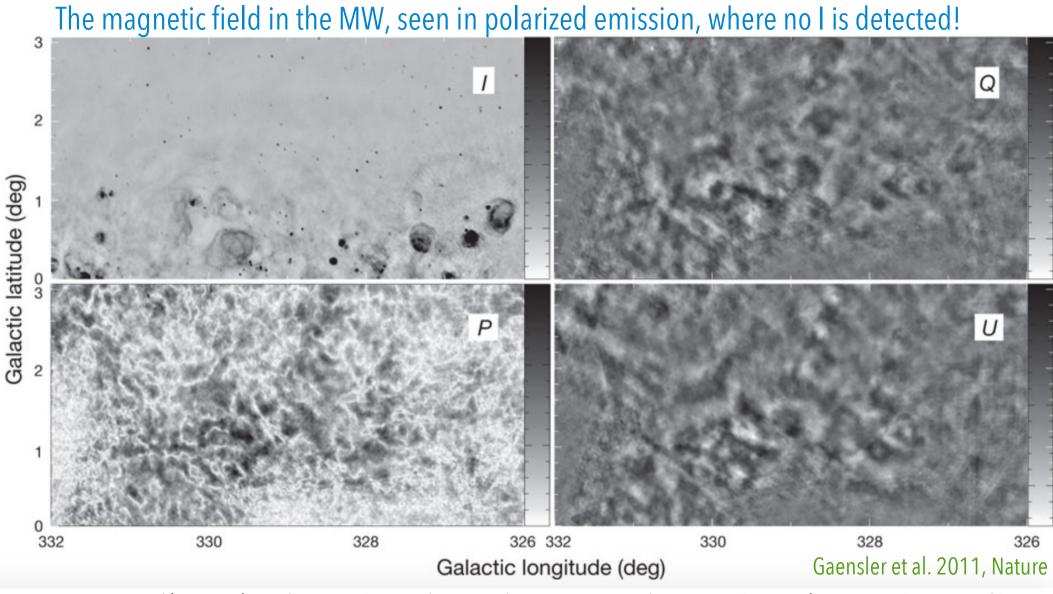
$$U = \frac{(E_R^i E_L^j - E_L^i E_R^j)}{2i}$$

$$V = \frac{(E_R^i E_R^j - E_L^i E_L^i)}{2}$$

for linearly polarized radiation:

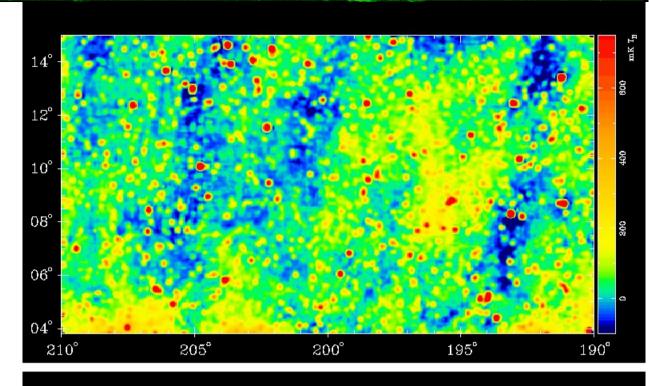
$$P = \sqrt{Q^2 + U^2}$$
  $\chi = 0.5 \times \text{atan2}(U, Q)$   $f_{pol} = \frac{P}{I}$ 

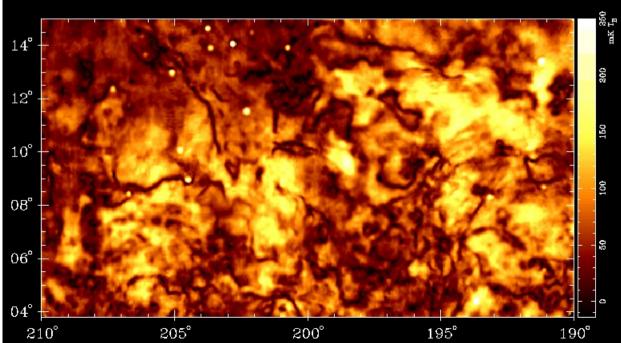
Images can be created in all Stokes parameters: I, U, Q, V, P,  $\chi$ , f



Images generated from a set of ATCA observations (1997 April – 1998 April,  $\Delta v$  = 96-MHz, centred on 1,384 $\Omega$ MHz). Mosaic of 190 pointings ( $\sim$  20 $\Omega$ min each),  $\sim$  uniform sensitivity of 0.8 $\Omega$ mJy/beam (Stokes I), 0.55 $\Omega$ mJy/beam (Stokes Q and Q), HPBW = 75". ATCA is an interferometer: it is not sensitive to structure on angular scales > 35 $\Omega$ mrcmin. Faint wisps can be seen, corresponding to the sharp edges of large-scale structures. However, the bulk of the smooth radio emission from Galactic cosmic rays is not detected. Imaging artifacts (grating rings & radial streaks) can be seen around a few very bright sources. Almost none of the structures seen in Q, Q and Q has any correspondence with any emission in Stokes Q; mottled structure = spatial fluctuations in Faraday rotation in the ISM.

The magnetic field in the MW, seen in polarized emission, where no I is detected!





Uyaniker et al. (1999)
Astron. Astrophys. Suppl. Ser. 138, 31-45
Images from Effelsberg single dish observations at 1.4 GHz.
Total intensity map of the small-scale emission (at top) and the polarized intensity map in the direction of the Galactic anticentre.